THERMOELECTRIC PROPERTIES OF NOVEL MICROSTRUCTURALLY MODIFIED CoSb$_3$ SKUTTERUDITE MATERIALS BY MINOR DOPANTS OF Mn, Hf, Al, Bi AND Yb

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Field of Study: Energy

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ABSTRACT

A key challenge in thermoelectrics research is obtaining materials with high electrical conductivity, a high Seebeck coefficient and low thermal conductivity. The essence of the phonon-glass electron-crystal (PGEC) concept is to synthesize ultimate thermoelectric materials that can conduct electricity like a crystal but insulate heat like a glass. In this respect, the skutterudite system is a promising material that utilizes the PGEC concept. The skutterudite system relies on a crystal “cage-like” structure with a rattler atom to allow simultaneous high electrical conductivity and low thermal conductivity.

In this work, the skutterudite compound was modified by adding Mn, Hf and Al\textsubscript{x} (x = 0.3, 0.6 and 2) to the binary skutterudite CoSb\textsubscript{3} and Al\textsubscript{x} (x = 0.1, 0.2 and 0.3), Bi\textsubscript{0.1} and Al\textsubscript{0.1}Bi\textsubscript{0.05} to the ternary skutterudite Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12}. The fabrication method utilized the mechanical alloying (MA) technique followed by the spark plasma sintering (SPS) process.

The addition of Mn, Hf, and Al\textsubscript{x} to the binary skutterudite CoSb\textsubscript{3} resulted in the formation of a polycrystalline skutterudite phase with Mn, Hf, and Al located in the grain boundaries. Moreover, the addition of Mn and Al led to an increase in the area fraction of the grain boundary compared with the addition of Hf, leading to an overall modification of the skutterudite microstructure. The addition of Mn, Hf, and Al had a significant effect on the lattice thermal conductivity of CoSb\textsubscript{3}, which was reduced by up to ~60% by the addition of Hf. However, the tradeoff for the microstructural modification of binary skutterudite is the relatively high electrical resistivity, thus resulting in moderate figures of merit (ZTs < 0.1). Therefore, grain boundary modification is an effective strategy to decrease thermal conductivity for this case.
A similar strategy for microstructural modification to introduce element-rich boundary regions was demonstrated to be effective for the addition of Al, Bi and Al$_{0.1}$Bi$_{0.05}$ to Yb$_{0.25}$Co$_4$Sb$_{12}$ ternary skutterudite. Al- and Bi-rich regions were found to exist at the nano-scale along the grain boundaries. An overall improvement in all three parameters was found in comparison to undoped CoSb$_3$. A figure of merit ZT value of more than unity (ZT = 1.36) was found using this strategy. Thus, this work is useful in deriving a pathway for improvement in thermoelectrics through microstructural modification.

An introductory investigation of n- to p-type inversion of the skutterudite thermoelectric material was demonstrated through the formulation of bulk skutterudite Al$_{0.3}$Co$_4$Sb$_{12}$. A wide range of Seebeck coefficient values from -251 μV/K at low temperature to +153 μV/K at high temperature with a critical point at 200 °C is reported. This formulation serves as the starting point for new fundamental investigations of the p-to n-type inversion phenomena in thermoelectrics. In addition, this finding indicates the potential of this material as a temperature switch.
ABSTRAK

Cabaran utama dalam termoelektrik ialah mendapatkan bahan yang mempunyai konduktiviti elektrik yang tinggi, pekali Seebeck yang tinggi, dan konduktiviti haba yang rendah. Inti pati konsep fonon-glass electron-kristal (PGEC) adalah untuk sintesis bahan termoelektrik terunggul yang mampu mengalirkan elektrik seperti kristal tetapi menebat haba seperti kaca. Dalam perkara ini, sistem skutterudit merupakan bahan harapan yang menggunakan konsep PGEC. Sistem skutterudit bergantung kepada struktur “sangkar” kristal yang mempunyai atom bergetar untuk membenarkan konduktiviti elektrikal yang tinggi dan haba yang rendah secara serentak.

Dalam kerja ini, pengubahsuaian kompaun skutterudit dengan tambahan Mn, Hf, dan Alx (x = 2, 0.6 dan 0.3) kepada skutterudit binari CoSb3, dan juga Alx (x = 0.1, 0.2 & 0.3), Bi0.1 dan Al0.1Bi0.05 kepada skutterudit ternari Yb0.25Co4Sb12 telah dijalankan. Kaedah fabrikasi yang digunakan ialah teknik pengaluan mekanikal (MA) diikuti dengan proses pensinteran cetusan plasma (SPS).

Penambahan Mn, Hf, dan Alx ke dalam skutterudit binari CoSb3 menghasilkan bentuk fasa skutterudit polihablur dengan kehadiran Mn, Hf, dan Al yang banyak di sempadan bijian. Di samping itu, penambahan Mn dan Al menyebabkan peningkatan luas pecahan sempadan bijian apabila dibandingkan dengan penambahan Hf, menyebabkan pengubahsuaian keseluruhan kepada mikrostruktur skutterudit. Secara nyata, penambahan Mn, Hf, dan Al memberi kesan ketara kepada kekisi konduktiviti haba CoSb3 yang mana dikerangkan sehingga ~60% dengan tambahan Hf. Walaubagaimanapun, trade-off pengubahsuaian mikrostruktur skutterudit binari ialah rintangan elektrikal yang agak tinggi, justeru mengakibatkan angka merit sederhana (ZTs< 0.1). Oleh itu, pengubahsuaian sempadan bijian telah ditunjukkan sebagai strategi efektif untuk mengurangkan konduktiviti haba dalam kes ini.
Strategi yang sama dalam pengubahsuaian mikrostruktur untuk memperkenalkan kawasan sempadan yang kaya elemen telah dibuktikan efektif dalam kes penambahan Al, Bi0.1 dan Al0.1Bi0.05 ke dalam Yb0.25Co4Sb12 skutterudit ternari. Kawasan yang kaya dengan Al dan Bi dijumpai berada di skala-nano di sepanjang sempadan bijian. Penambahbaikan menyeluruh dalam semua tiga parameter didapati apabila dibandingkan CoSb3 yang tidak didop. Nilai Angka merit ZT lebih daripada kesatuan (ZT = 1.36) telah didapati melalui strategi ini. Oleh itu, kerja ini berguna untuk menerbitkan laluan untuk penambahbaikan dalam termoelektrik melalui pengubahsuaian mikrostruktur.

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<thead>
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<tr>
<td>TE</td>
<td>Thermoelectric</td>
</tr>
<tr>
<td>$Z$</td>
<td>Thermoelectric figure of merit</td>
</tr>
<tr>
<td>$ZT$</td>
<td>Dimensionless thermoelectric figure of merit</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Seebeck coefficient</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Electrical conductivity</td>
</tr>
<tr>
<td>$T$</td>
<td>Temperature</td>
</tr>
<tr>
<td>$K$</td>
<td>Thermal conductivity</td>
</tr>
<tr>
<td>$PF$</td>
<td>Power factor</td>
</tr>
<tr>
<td>$\Delta V$</td>
<td>Voltage difference</td>
</tr>
<tr>
<td>$\Delta T$</td>
<td>Temperature difference</td>
</tr>
<tr>
<td>EMF</td>
<td>Electromotive force</td>
</tr>
<tr>
<td>$K_e$</td>
<td>Electrons and holes transporting heat</td>
</tr>
<tr>
<td>$K_L$</td>
<td>Phonons travelling through the lattice</td>
</tr>
<tr>
<td>$L$</td>
<td>Lorenz number</td>
</tr>
<tr>
<td>$K_B$</td>
<td>Boltzmann constant</td>
</tr>
<tr>
<td>$e$</td>
<td>Electron charge</td>
</tr>
<tr>
<td>PGEC</td>
<td>phonon-glass electron-crystal</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Electrical resistivity</td>
</tr>
<tr>
<td>HH</td>
<td>Half-Heusler</td>
</tr>
<tr>
<td>TNTs</td>
<td>Titanate nanotubes</td>
</tr>
<tr>
<td>PANI</td>
<td>Polyaniline</td>
</tr>
<tr>
<td>PTH</td>
<td>Polythiophene</td>
</tr>
<tr>
<td>PEDOT:PSS</td>
<td>Poly (3, 4-ethylenedioxythiophene): poly (styrenesulfonate)</td>
</tr>
</tbody>
</table>
PA : Polyacetylene
PPY : Polypyrrole
PC : Polycarbazoles
PPV : Polyphenylenevinylene
HMS : Higher manganese silicides
E_c : Conduction band
E_v : Valence band
E_f : Fermi level
E_g : Band gap
n : Carrier density
h : Planck’s constant
m^* : Effective mass of the charge carrier
C : Integration constant
v : Directional velocity component
j : Current density
E : Applied electric field
\mu : Charge-carrier mobility
l_e : Electron mean free path
l_p : Phonon mean free path
\rho_m : Mass density
v_s : Velocity of sound in the crystal
c : Specific heat of the crystal
m_e : Electron mass
TSO : Transparent semiconducting oxide
SPS : Spark plasma sintering
RSPs : Rapid solidification processes
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Term</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>Hardness</td>
</tr>
<tr>
<td>LAST</td>
<td>Lead-antimony-silver-tellurium</td>
</tr>
<tr>
<td>B</td>
<td>Bulk moduli</td>
</tr>
<tr>
<td>G</td>
<td>Shear moduli</td>
</tr>
<tr>
<td>E</td>
<td>Young’s moduli</td>
</tr>
<tr>
<td>v</td>
<td>Poisson ratios</td>
</tr>
<tr>
<td>a</td>
<td>Thermal expansion coefficient</td>
</tr>
<tr>
<td>CTE</td>
<td>Coefficient of thermal expansion</td>
</tr>
<tr>
<td>$T_m$</td>
<td>Melting temperature</td>
</tr>
<tr>
<td>HPT</td>
<td>High pressure torsion</td>
</tr>
<tr>
<td>TEGs</td>
<td>Thermoelectric generators</td>
</tr>
<tr>
<td>TECs</td>
<td>Thermoelectric coolers</td>
</tr>
<tr>
<td>COP</td>
<td>Coefficient of performance</td>
</tr>
<tr>
<td>MCC</td>
<td>Microclimate cooling</td>
</tr>
<tr>
<td>MS</td>
<td>Melt spinning</td>
</tr>
<tr>
<td>TEACs</td>
<td>Thermoelectric air conditioners</td>
</tr>
<tr>
<td>$\eta_{te}$</td>
<td>Energy-conversion efficiency</td>
</tr>
<tr>
<td>$T_h$</td>
<td>Hot-side temperature</td>
</tr>
<tr>
<td>$T_c$</td>
<td>Cold-side temperature</td>
</tr>
<tr>
<td>QW</td>
<td>Quantum-well</td>
</tr>
<tr>
<td>SUV</td>
<td>Sports utility vehicle</td>
</tr>
<tr>
<td>CNG</td>
<td>Compressed-natural-gas-fueled engine generator set</td>
</tr>
<tr>
<td>STEGs</td>
<td>Solar thermoelectric generators</td>
</tr>
<tr>
<td>SHP-TE</td>
<td>Glass evacuated-tube heat-pipe solar collectors</td>
</tr>
<tr>
<td>HSTE</td>
<td>Hybrid solar thermoelectric</td>
</tr>
<tr>
<td>HGS</td>
<td>Hybrid-generation-system</td>
</tr>
<tr>
<td>Abbreviation</td>
<td>Description</td>
</tr>
<tr>
<td>--------------</td>
<td>-------------</td>
</tr>
<tr>
<td>IR</td>
<td>Infrared</td>
</tr>
<tr>
<td>TMS</td>
<td>Thermoelectric microfluidic sensor</td>
</tr>
<tr>
<td>DI</td>
<td>Injecting deionized</td>
</tr>
<tr>
<td>RTGs</td>
<td>Radioisotope thermoelectric generators</td>
</tr>
<tr>
<td>GPHS</td>
<td>General-purpose heat-source</td>
</tr>
<tr>
<td>LES</td>
<td>Lincoln Experimental Satellite</td>
</tr>
<tr>
<td>MHW</td>
<td>Multi-hundred watt</td>
</tr>
<tr>
<td>JPL</td>
<td>Jet Propulsion Laboratory</td>
</tr>
<tr>
<td>ARPSs</td>
<td>Advanced Radioisotope Power Systems</td>
</tr>
<tr>
<td>CTMs</td>
<td>Cascaded thermoelectric modules</td>
</tr>
<tr>
<td>RPSs</td>
<td>Radioisotope power systems</td>
</tr>
<tr>
<td>MA</td>
<td>Mechanically alloying</td>
</tr>
<tr>
<td>XRD</td>
<td>X-ray Diffraction</td>
</tr>
<tr>
<td>SEM</td>
<td>Scanning electron microscope</td>
</tr>
<tr>
<td>EDX</td>
<td>Energy-dispersive X-ray spectroscopy</td>
</tr>
<tr>
<td>FIB</td>
<td>Focused ion beam</td>
</tr>
<tr>
<td>TEM</td>
<td>Transmission electron microscope</td>
</tr>
<tr>
<td>XPS</td>
<td>X-ray Photoelectron Spectroscopy</td>
</tr>
<tr>
<td>ESCA</td>
<td>Electron Spectroscopy for Chemical Analysis</td>
</tr>
<tr>
<td>I</td>
<td>Current</td>
</tr>
<tr>
<td>D</td>
<td>Thermal diffusivity</td>
</tr>
<tr>
<td>$C_p$</td>
<td>Specific heat</td>
</tr>
<tr>
<td>$\rho_d$</td>
<td>Density</td>
</tr>
<tr>
<td>T</td>
<td>Thickness</td>
</tr>
<tr>
<td>STA</td>
<td>Simultaneous Thermal Analysis</td>
</tr>
<tr>
<td>DSC</td>
<td>Differential scanning calorimetry</td>
</tr>
<tr>
<td>Acronym</td>
<td>Description</td>
</tr>
<tr>
<td>---------</td>
<td>---------------------------------</td>
</tr>
<tr>
<td>TG</td>
<td>Thermogravimetry</td>
</tr>
<tr>
<td>HV</td>
<td>Vickers hardness</td>
</tr>
<tr>
<td>F</td>
<td>Force</td>
</tr>
<tr>
<td>d</td>
<td>Average length</td>
</tr>
<tr>
<td>$\mu_H$</td>
<td>Hall mobility</td>
</tr>
<tr>
<td>LS</td>
<td>Low spin</td>
</tr>
<tr>
<td>HS</td>
<td>High Spin</td>
</tr>
<tr>
<td>HT-XRD</td>
<td>High temperature - X-ray Diffraction</td>
</tr>
<tr>
<td>SCO</td>
<td>Spin crossover</td>
</tr>
</tbody>
</table>
CHAPTER 1: INTRODUCTION

1.1 Background

The search for cleaner, more sustainable energy sources is an ever-growing global concern because of escalating energy costs and global warming associated with fossil fuel sources (Afshar et al., 2012; Kalkan et al., 2012; Omer, 2008; Thirugnanasambandam et al., 2010; Xi et al., 2007). Among the viable technologies for this purpose, thermoelectric (TE) energy converters are of increasing interest because these solid-state devices can transform heat given off from sources such as power plants, factories, motor vehicles, computers or even human bodies into electric power using the Seebeck effect (Fthenakis & Kim, 2010; Liu et al., 2010; Martín-González et al., 2013; Saidur et al., 2012; Shu et al., 2013; Vélez et al., 2012; Wang et al., 2011). The many advantages of this energy-conversion phenomenon include solid-state operation, the absence of toxic residuals, vast scalability, maintenance-free operation vis-à-vis the lack of moving parts or chemical reactions, and a long life span of reliable operation (Dai et al., 2011; Riffat & Ma, 2003; Tie & Tan, 2013; Ullah et al., 2013). Conversely, solid-state thermoelectric devices can also change electrical energy into thermal energy for cooling or heating using the Peltier effect. Compared to traditional refrigeration and heating mechanisms, solid-state thermoelectric energy converters have the advantage of simplicity; they produce no vibrations and are highly scalable. Furthermore, because TE devices use no refrigerants or working fluids, they may be expected to produce negligible direct emissions of greenhouse gases over their lifetimes (Tsubota et al., 2008). However, because of their low efficiency, current TE materials have found limited commercial application. A brief perusal of the possibilities is illustrated in Figure 1.1, where the different scales of energy generation that are represented are relevant to different applications (Pichanusakorn & Bandaru, 2010). The problem remains that the efficiency of today’s thermoelectric material is inadequate to compete with conventional power generation and refrigeration.
(Gao et al., 2006). Moreover, the growing need for alternative power sources is driving a growing interest in developing a new generation of thermoelectric materials. In order to become commercially competitive, novel thermoelectric materials will need to increase in efficiency by a factor of three over the present values (Zhan et al., 2006).

![Figure 1.1](image)

**Figure 1.1:** Thermoelectric materials can be put to use in various energy conversion applications, encompassing ten orders of magnitude in power, as illustrated above (Pichanusakorn & Bandaru, 2010).

### 1.2 Thermoelectric phenomena

Thermoelectric devices can convert thermal energy from a temperature gradient into electrical energy. This phenomenon was discovered in 1821 and is called the “Seebeck effect,” while the reverse counterpart of this phenomenon was discovered by Peltier in 1834 (Riffat & Ma, 2003). As knowledge of thermoelectrics increased, the most important discoveries were related to material properties. In 1911, Altenkirch derived the thermoelectric efficiency, now known simply as $Z$, or the thermoelectric figure of merit. The thermoelectric efficiency can be non-dimensionalized by multiplying by the absolute temperature $T$, which yields the most common form of thermoelectric efficiency, $ZT$, also known as the dimensionless figure of merit. This value is given as
$$ZT = \alpha^2 \sigma \frac{T}{K}$$  

where \( \alpha \) is the Seebeck coefficient, \( \sigma \) is the electrical conductivity, and \( K \) is the thermal conductivity. These three transport parameters \( \alpha, \sigma \) and \( K \) depend upon one another as a function of the band structure, carrier concentration and many other factors that are discussed later in this paper; Figure 1.2 illustrates the three main parameters, including the carrier concentration (Snyder & Toberer, 2008). In particular, \( \alpha \) and \( \sigma \) generally vary in a reciprocal manner, making any improvement in the figure of merit \( Z \) difficult (Cai et al., 2004). In addition, the electrical conductivity and the Seebeck coefficient are inversely related, so it is not generally possible to increase the thermoelectric power factor \( (PF = \alpha^2 \sigma) \) above a particular optimal value for a bulk material (Zide et al., 2006). However, ideal thermoelectric materials would have a high electrical conductivity to allow the conduction of electricity, which would create a potential difference across the sample, and a low thermal conductivity to maintain the temperature gradient between the hot and cold side (Bian & Shakouri, 2006). Early work in thermoelectrics resulted in very small values of \( Z \) because the materials being used (mostly metals) did not possess ideal thermoelectric properties; i.e., metals possess both high electrical conductivity and high thermal conductivity. Most traditional materials exhibit a correlation between electrical and thermal conductivity. A material that conducts electricity well, such as a metal, also conducts heat well, and a material that insulates heat, such as glass or ceramic, also insulates electricity (Snyder & Toberer, 2008).
Figure 1.2: Maximizing the efficiency ($ZT$) of a thermoelectric involves a compromise of thermal conductivity ($k$; plotted on the y axis from 0 to a top value of 10 W m$^{-1}$ K$^{-1}$) and Seebeck coefficient ($S$ or $\alpha$; 0 to 500 $\mu$V K$^{-1}$) with electrical conductivity ($\sigma$; 0 to 5,000 $\Omega^{-1}$cm$^{-1}$) (Snyder & Toberer, 2008).

Many years of effort to increase $ZT$ have not yet led to a fundamental breakthrough. In fact, the history of thermoelectric materials can be characterized by the progress in increasing $ZT$, as shown in Figure 1.3 (Zheng, 2008). Thus, for devices operating at room temperature ($T \approx 300$ K), traditional thermoelectric materials, such as bismuth telluride (Bi$_2$Te$_3$) and lead telluride (PbTe), possess values of $ZT \approx 1$ (Hochbaum et al., 2008). In recent years, work by Venkatasubramanian and his colleagues (Venkatasubramanian et al., 2001) and Harman et al. (Harman et al., 2002) using superlattices and quantum dots based on these materials has increased their room-temperature $ZT$ to ~2–2.4. These improvements in performance are primarily the result of a reduction in lattice thermal conductivity, and the thermoelectric power factor ($PF$) is largely unchanged. For practical purposes, a suitable high-performance TE material should have a $ZT$ of $> 4$, and the achievement of this goal has remained a formidable challenge (Gao et al., 2006). However, commercial materials are available with $ZT \approx 1$. 
1.3 Problem statement

To modulate high-performance the thermoelectric skutterudite material CoSb$_3$ with dopants, a lengthy synthetic process is required. The current state of the art for skutterudites in thermoelectrics usually consists of two pathways: a) a simple fabrication process (mechanically alloying + hot pressing) achieves a relatively low figure of merit ($ZT = 0.78$) (Liu et al., 2011), whereas b) the state-of-the-art processing (induction melting + long-term high-temperature annealing + cold pressing + long-term high-temperature annealing + ball milling + spark plasma sintering) achieves a higher figure of merit ($ZT = 1.7$) (Shi et al., 2011). Furthermore, some of the effective dopants, such as lanthanide elements, are costly. Thus, the scope of this work was to explore a high-performance skutterudite formulation using relatively simple fabrication methods.
1.4 Research objectives

For this thesis, the following objectives were defined to address the problem statement framed above:

1. To formulate new thermoelectric materials by incorporating Mn, Hf, and Al into CoSb$_3$ binary skutterudite and Al and Bi into Yb$_{0.25}$Co$_4$Sb$_{12}$ ternary skutterudite thermoelectric materials.

2. To fabricate high-performance skutterudite thermoelectric materials through a simple synthesis process of mechanical alloying and spark plasma sintering.

3. To characterize the microstructural, thermoelectric, charge transport, and mechanical properties and the thermal stability of the developed skutterudite materials.

4. To provide a physical framework for achieving improved $ZT$ in CoSb$_3$ skutterudites.

1.5 Organization of the dissertation

- The purpose of this study is presented in Chapter 1.
- Chapter 2 presents the background and literature review relevant to this study. The literature review primarily focuses on the parameters that affect the performance of thermoelectric materials and the thermoelectric applications.
- Chapter 3 describes the methodology and experimental study by explaining the steps of fabrication and testing.
- Chapter 4 deeply discusses the effect of minor doping on the skutterudite thermoelectric material formulation in terms of microstructure, thermoelectric properties, electronic properties, thermal stability and mechanical properties.
- General conclusions and potential future research are presented in Chapter 5.
CHAPTER 2: LITERATURE REVIEW

2.1 Thermoelectric properties

2.1.1 The Seebeck coefficient

A temperature difference between two points in a conductor or semiconductor results in a voltage difference between these two points. Stated differently, a temperature gradient in a conductor or semiconductor gives rise to a built-in electric field. This phenomenon is called the Seebeck effect or the thermoelectric effect (Sootsman et al., 2009). The Seebeck coefficient gauges the magnitude of this effect. The thermoelectric voltage developed per unit temperature difference in a conductor is called the Seebeck coefficient or thermopower ($\alpha = \Delta V/\Delta T$). Only the net Seebeck voltage difference between different metals can be measured (Zheng, 2008). In fact, it is via the Seebeck effect that thermoelectric devices can act as electrical power generators (Nolas et al., 1999). A schematic diagram of a simple solid-state thermoelectric refrigerator or power generator operating based on the Seebeck effect is shown in Figure 2.1.

![Figure 2.1: A thermoelectric modules illustrating the versatility of these materials for use in solid-state thermoelectric refrigeration or in power generation. The thermoelectric module is composed of an n-type and a p-type semiconducting material connected electrically in series through metallic electrical contact pads and thermally in parallel between ceramic ends (Nolas et al., 1999)](image)

The Seebeck coefficient is expressed in units of V/K (or, more commonly, $\mu$V/K or $\mu$V/°C). It has been found that only a combination of two different materials, a so-called
thermocouple, exhibits the Seebeck effect. For two leads of the same material, no Seebeck effect manifests, although both leads intrinsically possess a Seebeck coefficient, for reasons of symmetry. It is, however, present because the Seebeck effect is a bulk property and does not depend on either the specific arrangement of the leads or the material or the specific method of joining them (Van Herwaarden & Sarro, 1986). Metals have different thermoelectric sensitivities, or Seebeck coefficients. For example, iron has a Seebeck coefficient of 19 μV/°C at 0°C, which means that for every 1°C difference in temperature, a positive thermoelectric electromotive force (EMF) or (Seebeck voltage) of 19 μV is induced in iron at temperatures near 0°C. A negative thermoelectric electromotive force (EMF) can also be induced in a metal, so Seebeck coefficients can also have negative values. For example, constantan (a copper-nickel alloy) has a Seebeck coefficient of -35 μV/°C at 0°C. Generally, most metals possess Seebeck coefficients of 10 μV/K or less, but semiconductor materials are promising for the construction of thermocouples because they have Seebeck coefficients in excess of 100 μV/K. It should be noted that the relation between the Seebeck voltage and the temperature is linear only for small changes in temperature (Nolas et al., 1999). For larger temperature ranges, the relationship becomes non-linear. It is therefore important to state the temperature at which the Seebeck coefficient is being specified. However, thermopower ≥ 225 is required to achieve $ZT > 2$ (Tritt & Subramanian, 2006).

Recently, the interfacial thermoelectric effect has been generalized to include spin transport phenomena. The spin Seebeck effect refers to the generation of a spin voltage caused by a temperature gradient in a ferromagnet, which enables the thermal injection of spin currents from the ferromagnet into an attached nonmagnetic metal over a macroscopic scale of several millimeters. The main feature of the spin Seebeck device is that the output power is proportional to the length perpendicular to the temperature gradient. In addition, the paths of the heat current and charge current are separated in the
spin Seebeck device in dissimilarity to the charge Seebeck device (Adachi et al., 2013). Therefore, the spin Seebeck device could be a new trajectory to enhance the thermoelectric efficiency.

2.1.2 Thermal conductivity

A high-quality thermoelectric material must have a high electrical conductivity, a high thermopower, and a low thermal conductivity. Because the first two are determined only by the electronic properties of the material, they are often combined into the quantity $PF = \alpha^2 \sigma$, referred to as the ‘power factor.’ In contrast, the thermal conductivity $K = K_e + K_L$ in thermoelectrics is the sum of two contributions: (1) electrons and holes transporting heat ($K_e$) and (2) phonons travelling through the lattice ($K_L$) (Gonçalves et al., 2010). It then follows that the thermoelectric figure of merit can be maximized by maximizing the electrical conductivity and minimizing the thermal conductivity. However, there is a relation between the two: the Wiedemann-Franz law for electrons that obey degenerate and non-degenerate statistics ($K_B$ is the Boltzmann constant, and $e$ is the electron charge).

\[
\frac{K_e}{\sigma} = L_e T \tag{2-1}
\]

\[
L_e = \left(\frac{\pi^2}{3}\right) \left(\frac{K_B}{e}\right)^2 = 2.44 \times 10^{-8} \left(\frac{K^2}{V^2}\right) \tag{2-2}
\]

And

\[
L_s = 2 \left(\frac{K_B}{e}\right)^2 = 1.48 \times 10^{-8} \left(\frac{K^2}{V^2}\right) \tag{2-3}
\]

Increasing the electrical conductivity not only produces an increase in the electronic thermal conductivity but also usually decreases the thermopower; optimizing $ZT$ thus turns out to be a challenge. While the power factor can in some cases be increased by varying the concentration of charge carriers in the material, decreasing $K$ and $K_L$ is much
more problematic, especially for $K_L$, which is determined by the structure, rigidity, atomic masses, and other characteristics of the lattice (Dmitriev & Zvyagin, 2010). Because the $ZT$ values of the presently available materials are too low for cost-effective applications, various efforts have been made to improve them. The idea of reducing the $K_L$ of a compound by substituting the crystal lattice with an amorphous (glass-like) structure has been suggested, and the phonon-glass electron-crystal (PGEC) concept, which was first introduced by Slack and discussed in detail in a review by Nolas et al. (1999) and has become a general guideline for the development new thermoelectric materials, is at the heart of the investigation into the skutterudite material system for thermoelectric applications. A PGEC material would possess electronic properties similar to those normally associated with a good semiconductor single crystal but would have thermal properties akin to those of an amorphous material.

It is believed that the ideal thermoelectric material would have regions of its structure composed of a high-mobility semiconductor, which provides the electron-crystal electronic structure, interwoven with a phonon glass. The phonon-glass region would be ideal for hosting dopants and disordered structures without disrupting the carrier mobility in the electron-crystal region (Wan et al., 2010). The thermal conductivity of a semiconductor material is related to its position in the periodic table, i.e., for a larger mean atomic weight, the thermal conductivity is lower. This behavior has been attributed to the increase in density causing the velocity of sound in the crystal to decrease, leading to a subsequent decrease in thermal conductivity (Bulusu & Walker, 2008).

The most widely used commercial thermoelectric material is bulk Bi$_2$Te$_3$ and its alloys with Sb, Se, and so on, which exhibit $ZT \approx 1$. It is difficult to scale bulk Bi$_2$Te$_3$ to large-scale energy conversion, but fabricating synthetic nanostructures for this purpose is even more difficult and expensive. Conversely, the most common semiconductor, Si, is abundant and widely used in the electronics industry, and a large industrial infrastructure
exists for the low-cost and high-yield processing of Si. Bulk Si, however, has a high $K$ ($\sim 150$ Wm$^{-1}$ K$^{-1}$ at room temperature), yielding $ZT \approx 0.01$ at 300 K (Ma et al., 2008). Increasing $ZT$ via the reduction of $K$, by reducing the lattice contribution to the thermal conductivity, is a powerful concept. The most important factors that can aid in accomplishing this are (i) the use of compounds with complex crystal structures, (ii) the presence of heavy atoms weakly bonded to the structures, (iii) the existence of inclusions and/or impurities, (iv) the formation of solid solutions and (v) the existence of a large number of grain boundaries (Gonçalves et al., 2012).

The introduction of nanostructure has also become a potential tool for reducing $K$ and consequently increasing $ZT$. This concept has revolutionized the field of TE because, the utilization of nanostructures has led to the achievement of $ZT$ values of approximately 1-2 compared to < 1 for bulk materials. The Nanostructured Bi$_x$Sb$_{2-x}$Te$_3$ have been shown to exhibit significantly improved $ZT \approx 1.4$ at 100 °C, mostly because of the reduced $K_L$ (Ma et al., 2008). However, it is difficult to scale up these superlattices for large-volume energy-conversion applications because of limitations in both heat transfer and cost. Joshi et al. (Joshi et al., 2008) investigated the enhanced thermoelectric figure of merit in nanostructured p-type silicon germanium bulk alloys and found that this $ZT$ enhancement is most likely attributable to the increased phonon scattering at the grain boundaries and crystal defects formed by lattice distortion, with some contribution from the increased electron power factor at high temperatures.

### 2.1.3 Electrical resistivity ($\rho$)

Electrical resistivity is an important material-dependent property that is usually a function of temperature. The value of $\rho$ at room temperature is indicative of whether a material is an insulator (an insulator ($\rho$ is on the order of $10^6$ Ω.m or more) or a metal ($\rho$ is on the order of $10^{-6}$ Ω-m or less). In the latter case, if the lattice were perfect, the electron
would travel infinitely through it, and the material would only exhibit finite conductivity because of the thermal motion of the lattice and the effect of impurities (Bulusu & Walker, 2008). The resistivity of a semiconductor material falls between the metal and insulator regimes. It has been found that the optimum range of electrical resistivity for a thermoelectric material is from $10^{-3}$ to $10^{-2}$ $\Omega\cdot$m (Cadoff & Miller, 1960). Variations in the electrical resistivity of a semiconductor depend on changes in the carrier concentration and the mean free path of the charge carriers. The charge carriers are reflected/scattered by the surface of the material when they reach it (Das & Ganesan, 1998). To achieve low electrical resistivity in semiconductors, the lattice should have nearly infinite conductance at low temperatures, but in reality, the conductivity of semiconductors is very low at low temperatures because of the limited number of free electrons (Bulusu & Walker, 2008). Moreover, the analysis of the temperature dependence of the electrical resistivity in intermetallic compounds is a powerful tool for obtaining information regarding the intrinsic properties of these materials. Depending on the temperature range considered, one can draw certain conclusions regarding the scattering of electrons on the thermal excitations of the lattice (Kowalczyk et al., 2008).

2.2 Categories of TE materials

Thermoelectric materials comprise a huge family, including various materials from semimetals and semiconductors to ceramics, containing various crystalline forms from monocrysrtals and polycrystals to nanocomposites and covering varying dimensions from bulk, films and wires to clusters. Recently, certain polymers have also been shown to exhibit interesting thermoelectric material properties.

2.2.1 Metal-based thermoelectrics

The history of applications of thermoelectric materials is strongly associated with their efficiency. The earliest application of the thermoelectric effect was in metal
thermocouples, which have been used to measure temperature and radiant energy for many years (Zheng, 2008). However, metals possess very high electrical conductivity and very high thermal conductivity. Several TE materials containing heavy metals such as Bi, Sb, Pb and Te have been developed so far; these materials are mostly toxic and unstable at high temperatures (~1000 K) (Wang et al., 2008). Therefore, metal oxides that exhibit good TE performance are in high demand because metal oxides are environmentally friendly and essentially stable at high temperatures (Wang et al., 2008). (Watanabe et al., 2012) measured the temperature dependence of the electrical resistivity and the thermoelectric power of (Ni$_{1-x}$M$_x$)Mn$_2$O$_4$ (M = Zn and Mg, x = 0, 0.1 and 0.2), and they reported that the activation energy for electrical conduction is increased above a certain temperature (~450 °C). In the low-temperature region, the absolute value of the thermoelectric power is increased by Mg substitution, and the thermoelectric powers of all samples are found to change sign from negative to positive as the temperature increases.

To obtain phonon-glass electron-crystal PGEC materials, the idea of a complex structure, which imagines a material with distinct regions that each provide different functions, has been advanced (Wan et al., 2010). Two relatively new material classes are widely regarded as PGEC materials, namely, the clathrates and the filled skutterudites. Clathrates are periodic solids in which tetrahedrally coordinated atoms form cages that surround a metal atom (Iversen et al., 2000). Clathrate I materials have the general formula A$_8$E$_{46}$, with A = Na, K, or Ba and E = Al, Ga, In, Si, Ge, or Sn. Clathrates II and III have idealized formulas of A$_{24}$E$_{136}$ and A$_{30}$E$_{172}$, respectively, and exist with the same A and E elements; see Figure 2.2 (Kleinke, 2010). The low thermal conductivities for semiconducting clathrates are attributed to resonant scattering of the acoustic heat-carrying phonons by the guest atoms. The localized low-frequency vibration mode of the guest atoms is expected to cut through the acoustic branches, which decreases the number
of acoustic phonon modes and effectively limits the heat transport (Christensen et al., 2006), i.e., the enhanced vibration of the guest atoms A causes a flattening of the phonons bands, lowering the velocity of the phonons, which significantly contributes to the low thermal conductivity of these materials (Kleinke, 2010). However, a few studies have investigated clathrate structures, and all have reported $ZT < 1$ (Anno et al., 2012).

**Figure 2.2:** Crystal structure of cubic $\text{Ba}_8\text{Ga}_{16}\text{Si}_{30}$. All three E sites are mixed occupied by Ga and Si (Kleinke, 2010).

The essence of the PGEC concept is to synthesize semiconducting compounds in which one of the atoms is weakly bonded in an oversized atomic cage. In this sense, the skutterudite system is a promising material for thermoelectric applications (Kim et al., 2003). The basic family of binary semiconducting compounds has been widely investigated (Mi et al., 2006; Yang et al., 2010); a skutterudite structure generally has the form $\text{MX}_3$, where $\text{M}$ is the transition metal element, Co, Rh, or Ir, and $\text{X}$ is the pnictogen element, such as P, As, or Sb. Examples of skutterudite structures are $\text{CoP}_3$, $\text{CoAs}_3$, $\text{CoSb}_3$, $\text{RhP}_3$, $\text{RhAs}_3$, $\text{RhSb}_3$, $\text{IrP}_3$, $\text{IrAs}_3$ and $\text{IrSb}_3$ (Nolas et al., 1999).

For several years, efforts have focused on the preparation and characterization of ternary skutterudites that are isoelectronic to the binary skutterudites (Vaqueiro et al.,
Ternary skutterudites can be obtained either by substitution at the anion site, X, by a pair of elements from groups IV and V (e.g., CoSb$_{3-y}$Sn$_y$) (Kim et al., 2007) or by isoelectronic substitution at the cation site, M, by a pair of elements from subgroup VIII (e.g., Fe$_x$Co$_{4-x}$Sb$_{12}$) (Ur et al., 2007). Binary skutterudites are known for their high electron mobilities and favorable Seebeck coefficients but, unfortunately, have large values of lattice thermal conductivity. However, up to date the highest Figure of merit $ZT$ of 0.15 for high purity CoSb$_3$ nanostructured TE material at 650 K was achieved by Khan et al. (2014).

Filling the voids with elements that are loosely bond and thus able to “rattle,” thereby providing a phonon-scattering mechanism in the skutterudite structure, provides a possible solution to this obstacle (Alboni et al., 2007). Filling the interstitial voids in the structure with foreign atoms, especially alkaline-earth atoms (Matsuoka et al., 2006; Kwan-Ho Park & Kim, 2010), rare earth atoms (Allen et al., 2006; Kim et al., 2004; Rogl et al., 2011; Sklad et al., 2010) and other ions (Grytsiv et al., 2003; Jung et al., 2008), is an effective method of reducing the thermal conductivity while maintaining the electrical conductivity and the Seebeck coefficient of CoSb$_3$-based skutterudites (Lu et al., 2010). Many such efforts toward filling skutterudites have been reported: (i) partially filled skutterudite (e.g., La$_{0.1}$Co$_4$Sb$_{12}$) (Liu et al., 2006), (ii) filled skutterudite (e.g., CeFe$_4$Sb$_{12}$) (Ravot et al., 2001), (iii) double-filled skutterudite (e.g., Ba$_x$Ce$_y$Co$_4$Sb$_{12}$) (Bai et al., 2009) and (iv) multiple-filled skutterudite (e.g., Yb$_{0.2}$Ce$_{0.15}$In$_{0.2}$Co$_4$Sb$_{12}$) (Ballikaya et al., 2012). Meanwhile, filling the core of the cage-like framework, as shown in Figure 2.3, via doping (Chakoumakos & Sales, 2006) can also serve to reduce the thermal conductivity (Deng et al., 2011). The substitution of antimony by Se and Te can influence the electronic structure and electrical properties of the material; in particular, such substitution leads to a substantial change in the carrier masses and enhanced scattering of phonons on impurities (Wojciechowski et al., 2003). Generally, n-type CoSb$_3$ is prepared...
by substituting Fe, Ni, Pd or Pt into Co sites, which enhances the mass fluctuation scattering (Kitagawa et al., 2005; Peng et al., 2004), thereby significantly reducing the lattice thermal conductivity from its original value. However, investigations of filled skutterudite as a promising candidate for power-generation applications in the temperature range of 500–800 K (Yu et al., 2013) have led to observations of large $ZT$ values for many n-type filled skutterudites, such as 1.3 at 800 K for $\text{Ba}_{0.08}\text{Yb}_{0.14}\text{Eu}_{0.10}\text{Co}_4\text{Sb}_{12}$ (Shi et al., 2009) and 1.7 at 850 K for $\text{Ba}_{0.08}\text{La}_{0.03}\text{Yb}_{0.04}\text{Co}_4\text{Sb}_{12}$ (Shi et al., 2011).

Figure 2.3: Crystal structure of filled skutterudite (Chakoumakos & Sales, 2006).

Among the numerous TE materials, half-Heusler (HH) alloys have attracted considerable attention because of their appealing electrical transport properties and their relatively high Seebeck coefficients in addition to their rich elemental combinations (Zou et al., 2013). These alloys have three components that may originate from different elemental groups or may be a combination of elements in the same group. Two of the groups are composed of transition metals, and the third group consists of metals and metalloids. The chemical formula of half-Heusler alloys is $\text{XYZ}$, where X, Y, and Z can be selected from many different elemental groups (for example, X = Ti, Zr, Hf, V, Mn, or Nb; Y = Fe, Co, Ni, or Pt; Z=Sn or Sb). The crystal structures of the ternary
intermetallic compounds usually are of the cubic MgAgAs type (space group F-43m) (Wang et al., 2010). Figure 2.4 shows the crystal structure of half-Heusler compounds XYZ (Kawaharada et al., 2004). These compounds have a narrow band gap on the order of 0.1–0.2 eV at the Fermi level and have garnered interest because of their potential as thermoelectric materials (Shutoh & Sakurada, 2005). Their associated large effective masses lead to several characteristics, including large thermoelectric power factors, large Seebeck coefficients (250 μVK⁻¹) at room temperature, moderate electrical resistivity (1–10 μΩm) and high thermal conductivity (~10 Wm⁻¹K⁻¹) at room temperature (Lee & Chao, 2010). MNiSn and MCoSb (M = Ti, Zr, Hf) compounds are of great interest among the half-Heusler family because of their good thermoelectric properties. The state-of-the-art ZT values of MNiSn (M = Ti, Zr, Hf) compounds are close to unity (Fu et al., 2013). However, most efforts thus far have concentrated on the optimization of the thermoelectric performance of n-type half-Heusler alloys. The search for promising p-type half-Heusler materials that can be coupled to existing high-performance n-type half-Heusler alloys for high-temperature thermoelectric power generation has only been initiated in the past decade (Maji et al., 2010).

![Figure 2.4: Crystal structure of the half-Heusler type compounds (Kawaharada et al., 2004).](image)
Typically, other metals have been used as dopants. β-Zn₄Sb₃ has a hexagonal rhombohedral crystal structure, space group R3C with 66 atoms per unit cell. With its complex structure low thermal conductivity values can be expected (Zhu et al., 2000). The low-temperature structural phase transitions of Bi-, Pb-, In- and Sn-doped samples of thermoelectric Zn₄Sb₃ have been characterized on crystals grown from molten metal fluxes by Nylén et al. (2007), and they observed that when preparing β-Zn₄Sb₃ in the presence of metals with low melting points (Bi, Sn, In, and Pb), the additional metal atoms are unavoidably incorporated in small concentrations (0.04–1.3 wt%), act as dopants and alter the subtle balance between Zn disorder and Zn deficiency in Zn₄Sb₃, which has dramatic consequences for its low-temperature structural behavior.

In general, metals with poor conductivity are good candidates for providing enhanced values of thermoelectric power. It might be important to consider that most metallic materials contain inclusions, which can be either metallic or non-metallic. Inherent to the elaboration process, they are distributed inside the materials. These inclusions in alloys reduce their mechanical strength and resilience, are detrimental to surface finish and increase porosity, and they have a tendency to increase corrosion (Carreon, 2013). Furthermore, they act as stress enhancers and can cause the premature failure of in-service components.

2.2.2 Ceramics
Over the past two decades, from the discovery of the first ceramic thermoelectric material, many efforts have been put forth to obtain high-performance thermoelectric materials for application in energy-conversion systems (Ferreira et al., 2012). To date, the doped alloy TE materials based on Bi₂Te₃ are the best-known ones, and they exhibit $ZT \approx 1$ at room temperature. However, because they are easily oxidized and vaporized, these TE alloy materials cannot be used for applications at high temperatures in air (Liu et al.,
Thermoelectric oxide materials have drawn much attention because of their good thermal stability at high temperatures and their low toxicity compared to conventional intermetallic alloys (Wang et al., 2010). However, research seeking efficient thermoelectric materials often involves no conventional semiconductors. In this sense, oxide compounds such as NaCo$_2$O$_4$, LaCoO$_3$, (ZnO)$_m$In$_2$O$_3$, BaSnO$_3$, BaPbO$_3$, Ca$_3$Co$_4$O$_9$, Sr$_{1-x}$Nd$_x$TiO$_3$ and Bi$_2$Ca$_2$Co$_2$O$_x$ are promising candidates for thermoelectric materials because of their transport properties and their physical and chemical stability (Constantinescu et al., 2013; Kenfaui et al., 2010; Li & Li, 2011; Liu et al., 2010; Tajima et al., 2001; Wang et al., 2012; Yasukawa & Kono, 2006; Yasukawa et al., 2010).

The addition of titanate nanotubes (TNTs) (2 vol%) fabricated via the pressureless sintering method has been found to enhance the $ZT$ value of Nb-doped SrTiO$_3$ polycrystalline ceramic to approximately 0.14 at 900 K (Wang et al., 2010). (Ca$_{1-x}$Sr$_x$)$_3$Co$_4$O$_9$ polycrystalline has been fabricated by using spark plasma sintering method to substitute Ca by Sr, and the result demonstrated that the figure of merit $ZT$ achieves 0.22 at 1000K for the composition (Ca$_{0.995}$Sr$_{0.005}$)$_3$Co$_4$O$_9$ (Delorme et al., 2011). However, the fabrication of modules based on oxide materials has only recently begun to emerge, and there exist very few reports concerning the performance of these materials (Noudem et al., 2008). The oxide nature of the thermoelectric elements and the processing specifications, which involve very high temperatures, make the fabrication a difficult task and different from that of conventional thermoelectric modules (Noudem et al., 2008).

2.2.3 Polymers

Among the various categories of thermoelectric materials, a great deal of attention has recently been paid to organic TE materials, particularly since the discovery of conducting polymers (Tsai et al., 2011). In this regard, polymers are very attractive because they are
light, flexible, and suitable for room-temperature applications and because they generally require relatively simple manufacturing processes (i.e., spin coating and inkjet printing) compared to semiconductor-based thermoelectrics. Polymers are intrinsically poor thermal conductors, which makes them ideal for use as thermoelectrics, but their low electrical conductivity, Seebeck coefficient, and stability have hampered their use in thermoelectric applications (Choi et al., 2011). However, compared to inorganic TE materials, organic or polymer TE materials exhibit several inherent advantages, such as potentially low cost because of the abundance of carbon resources, simple synthesis in general, abundant electron-energy bands through modulation, simple processing into versatile forms, high energy density, and low $k$, which may be of great importance for their potential TE applications.

The physical and chemical properties of certain polymers are tunable within a fairly large range of modifications of their molecular structures (Yue & Xu, 2012). The ionic conducting polymers, such as poly(3,4-ethylenedi-oxythiophene):poly(styrenesulfonate) (PEDOT:PSS), which possess high electrical conductivity and intrinsically low thermal conductivity, are considered to be the most promising novel organic TE materials (Tsai et al., 2011). In a two-component nanocomposite, the selection of a conducting polymer and an inorganic thermoelectric material may yield high thermoelectric power and high electrical conductivity of the material. Because these properties are dependent on the particle size and morphology, it is interesting to map the relation between the structural and electrical properties of the material.

Recently, various researchers have attempted to prepare nanocomposites/hybrids/heterostructures of inorganic thermoelectrics with conducting polymers (Chatterjee et al., 2009). Table 2.1 summarizes the electrical conductivity $\sigma$, Seebeck coefficient $\alpha$, thermal conductivity $k$ and power factor $PF$ as well as the highest
ZT value of a few typical polymer and polymer-inorganic TE nanocomposites. Du et al. (Du et al., 2012) reviewed the research progress concerning conducting polymers and their corresponding TE nanocomposites, and their primary focus was TE nanocomposites based on conducting polymers such as polyaniline (PANI), polythiophene (PTH), and poly (3, 4-ethylenedioxythiophene): poly (styrenesulfonate) (PEDOT:PSS), as well as other polymers such as polyaniline (PANI), polythiophene (PTH), polycarbazoles (PC) and polyphenylenevinylene (PPV); these materials appear to have great potential for producing relatively low-cost and high-performance TE materials, and the authors reported that in polymer and polymer-inorganic TE nanocomposites, the value of the Seebeck coefficient typically ranges from −4088 to 1283 μV/K, the electrical conductivity ranges from $10^{-7}$ to $10^4$ S/cm, and the thermal conductivity ranges from 0.02 to 1.2 W/mK. However, it has been demonstrated that the transport properties of conducting polymers are greatly influenced by the process of doping with various materials.
Table 2.1: The electrical conductivity $\sigma$, Seebeck coefficient $\alpha$, thermal conductivity $k$ and power factor $PF$ as well as the highest $ZT$ value of a few typical polymer and polymer-inorganic TE nanocomposites.

<table>
<thead>
<tr>
<th>Materials</th>
<th>$\sigma$ (S/cm)</th>
<th>$\alpha$ (µV/K)</th>
<th>$K$ (W/mK). Maximum $PF$ (µW/mK$^2$) or $ZT$</th>
</tr>
</thead>
<tbody>
<tr>
<td>PANI</td>
<td>$\sim 10^{-2}$-320</td>
<td>$\sim$ -16-225</td>
<td>$K$, $\sim 0.02$-$0.542$, $ZT_{max}$, $1.1\times10^{-2}$ at 423K</td>
</tr>
<tr>
<td>PANI-inorganic TE nanocomposites</td>
<td>0-140</td>
<td>$\sim$ -30-626</td>
<td>$\kappa$, 0.25-1.2</td>
</tr>
<tr>
<td>PTH</td>
<td>$\sim 10^{-2}$-10$^3$</td>
<td>$\sim$ 10-100</td>
<td>$K$, 0.028-$0.17$, $ZT_{max}$, $2.9\times10^{-2}$ at 250K</td>
</tr>
<tr>
<td>PTH -inorganic TE nanocomposites</td>
<td>7.1-8.3</td>
<td>-56-1283</td>
<td>$PF_{max}$, $2.5\times10^{-2}$</td>
</tr>
<tr>
<td>PEDOT:PSS</td>
<td>0.06-945</td>
<td>8-888</td>
<td>$K$, 0.34, $ZT_{max}$, $1.0\times10^{-2}$ at 300K</td>
</tr>
<tr>
<td>PEDOT-Tos</td>
<td>$6\times10^{-4}$-300</td>
<td>40-780</td>
<td>$K$, 0.37, $ZT_{max}$, 0.25 at RT</td>
</tr>
<tr>
<td>PEDOT:PSS-inorganic TE inorganic nanocomposites</td>
<td>0-400</td>
<td>$\sim$ -125-167</td>
<td>$K$, 0.22, $ZT_{max}$, 0.10 at RT</td>
</tr>
<tr>
<td>PPY</td>
<td>0-340</td>
<td>-1-40</td>
<td>$K$, 0.2, $ZT_{max}$, $3\times10^{-2}$ at 423K</td>
</tr>
<tr>
<td>PA</td>
<td>$\sim 1.53\times10^{-3}$-$2.85\times10^{-4}$</td>
<td>$\sim$ 0.5-1077</td>
<td></td>
</tr>
<tr>
<td>PC</td>
<td>$\sim 4.0\times10^{-5}$-$5\times10^{-2}$</td>
<td>4.9-600</td>
<td>$PF_{max}$, 1.9</td>
</tr>
<tr>
<td>PMeOPV</td>
<td>46.3</td>
<td>39.1</td>
<td>$PF_{max}$, 7.1</td>
</tr>
<tr>
<td>P(ROPV-co-PV)(RO-MeO,EtO and BuO)</td>
<td>183.5-354.6</td>
<td>21.3-47.3</td>
<td>$K$, 0.25-$0.80$ (estimated), $ZT_{max}$, $9.87\times10^{-2}$ at 313K</td>
</tr>
<tr>
<td>Others polymer-inorganic TE nanocomposites (polymer/carbon nanotube with different contents of CNT)</td>
<td>$\sim$0-48</td>
<td>$\sim$ 40-50</td>
<td>$K$, 0.18-$0.34$, $ZT_{max}$, 0.006 at RT</td>
</tr>
</tbody>
</table>

(Du et al., 2012)
2.2.4 Semiconductors

Since the late 1950s, research concerning semiconducting thermoelectric devices has been applied for terrestrial cooling and power generation and later for space power generation because of their competitive energy conversion compared to other types of small-scale electric power generators (Zhang et al., 2009). Semiconductor thermoelectric power generation, which is based on the Seebeck effect, has very interesting capabilities with respect to conventional power-generation systems (Chen et al., 2005). During the 1990s, there was a heightened interest in the field of thermoelectrics driven by the need for more efficient materials for electronic refrigeration and power generation. Because of the use of semiconductor materials for thermoelectric applications, there has been a considerable effort to improve the figures of merit (ZT) of these materials to greater than 3 to make them commercially viable. Semiconductor materials are promising for the construction of thermocouples because they have Seebeck coefficients in excess of 100 μVK\(^{-1}\) (Dughaish, 2005), and the only way to reduce K without affecting α and σ in bulk materials, thereby increasing ZT, is to use semiconductors of high atomic weight, such as Bi\(_2\)Te\(_3\) and its alloys with Sb, Sn, and Pb. A high atomic weight reduces the speed of sound in the material and thereby decreases the thermal conductivity (Majumdar, 2004).

A solid-state or semiconductor electronics component, for example, can perform well and reliably for many years when it is operating at or near the ambient temperature (Alam & Ramakrishna, 2013). Intermetallic compounds such as Mg\(_2\)X (X = Si, Ge, Sn) and their solid solutions are semiconductors with the antifluorite structure and have been proposed as good candidates for high-performance thermoelectric materials because of their superior features such as large Seebeck coefficients, low electrical resistivities, and low thermal conductivities (Tani & Kido, 2005). For example, higher manganese silicides (HMS) are proven to be promising candidates as p-type thermoelectric material in the
temperature range of 400–700 K (Saleemi et al., 2015). However, the best-ZT materials are found to be heavily doped, small-band-gap semiconductors.

2.3 Fabrication process of the skutterudite TE materials

The best results of mechanical processing of skutterudites involve multiple steps, which can be generalized as follows:

- Melting the powder or/and the shots using arc furnace,
- Formation of ingots using the molten material above,
- Grinding of the ingots into fine powder,
- Loading of the powder into quartz ampoules,
- Sealing of the ampoules and heating in a furnace to 1473 K at 5 K/min,
- Maintain at 1473 K for 1 h,
- Cooling to 1073 K at 5 K/min,
- And, finally annealing at 1073 K for 50 h or more (Kawaharada et al., 2001).

Examples of high performing filled skutterudites have shown a high Figure of merit (ZT ≥ 0.9) when prepared using the process described above. The addition of filler atoms have served to act as rattler atoms which consequently reduce the thermal conductivity and consequently improve the figure of merit. A composition of Eu$_{0.27}$Co$_4$Sb$_{12}$ were synthesized by melting method and sintered by spark plasma sintering technique has shown a maximal value of 0.9 at 850 K (Pei et al., 2008).

Mallik et al. (2009) have shown that utilizing the above and including nano-inclusions have further enhanced the ZT value. For example, a maximum ZT value of 0.96 was achieved for In$_{0.4}$Co$_4$Sb$_{12}$ with InSb nano-inclusions by using vacuum induction melting and long annealing process. These results indicate that a small amount of secondary
phases in the skutterudite system will not prevent high TE performance. In addition, it may increase the phonon scattering hence decrease the thermal conductivity.

The multi-filling approach was then exploited by other workers to further improve the Figure of Merit. For example, The Yb atom is one of the most effective species among the lanthanide atoms for filling the skutterudite voids due to their large atomic mass, radius and it is intermediate valence state. Yb-filled skutterudite has been optimized with different combinations of Ce and In by Ballikaya et al. (2012) have achieve high values of ZT. The highest ZT value of 1.43 was achieved for Yb$_{0.2}$Ce$_{0.15}$In$_{0.2}$Co$_4$Sb$_{12}$ triple-filled skutterudite at 800 K containing nanoinclusions of Yb$_2$O$_3$ and Sb. The process which enabled this high Figure of Merit was melting–annealing followed by spark plasma sintering to prepare the samples.

On the other hand, the fast fabrication process such as mechanical alloying followed by hot pressing or spark plasma sintering has always shown a ZT < 0.9. Starting from elemental powder mixtures of La$_x$Co$_4$Sb$_{12}$ were prepared via mechanical alloying (MA) and spark plasma sintering (SPS) by Liu et al. (2006) and the maximum ZT value was 0.3425 when x = 0.9 at 500 °C. To enhance the thermoelectric performance of fast prepared element the addition of none-inclusions in the lattice system would be a good approach, which is the central theme explored in this thesis. The composition of Yb$_{0.2}$Co$_4$Sb$_{12}$ with PbTe inclusions has shown a higher ZT value of 0.78 at 700 K when prepared by the ball-milling and hot-pressing process (Liu et al., 2011). This is the record ZT achieved using fast fabrication process, prior to the work discussed in this thesis. Therefore, the short time of fabrication process needs extra effort in term of the microstructure modification to overcome the low ZT of < 1.
2.4 Governing parameters for thermoelectric material selection: Intrinsic material properties

2.4.1 Energy gap and band structure in semiconductors

In a solid, electrons exist at energy levels that combine to form energy bands. A simplified energy-band diagram is shown in Figure 2.5. The top band is called the conduction band $E_c$, and the next lower one is called the valence band $E_v$. The Fermi level $E_f$ (the hypothetical level of potential energy for an electron inside a crystalline solid and a term used to describe the highest of the collection of electron energy levels at a temperature of absolute zero) in intrinsic semiconductors lies essentially halfway between the valence and conduction bands. The region between the valence band and the conduction band is called the forbidden band, where, ideally, no electrons exist (Ozpincici & Tolbert, 2003). For a conductor such as copper, no forbidden band exists, and the energy bands overlap. For an insulator, conversely, this band is so wide that the electrons require a great deal of energy to move from the valence band to the conduction band. For semiconductors, the gap of the forbidden band is smaller than for an insulator. If the electrons in the valence band are excited externally, they can move to the conduction band. In the valence band, they have an energy of $E_v$. To move to the conduction band, they require an amount of energy $E_g = E_c - E_v$, where $E_g$ is the band gap (Ozpincici & Tolbert, 2003).
Since 1954, the control of the energy gap via the effect of the carrier concentration has become one of the methods of greatest interest for controlling the properties of semiconductors. This phenomenon, however, has also been used to analyze the degree of impurity in semiconductor crystals (Omar & Gorges, 2006). A great improvement of electrical properties is closely related to the narrowing of the band gap, though precipitated impurity phases can influence the measured band-gap value (Gao et al., 2012). Table 2.2 lists some semiconducting elements and compounds alongside their band gaps at 300 K (Hummel, 2011). Because electrical transport properties are closely related to the electronic states near the highest valence band and the lowest conduction band for some compounds, it is reasonable to focus on the energy bands near the Fermi level. The band-gap energy is expected to decrease as the atomic number of the constituent atoms increases. The atomic potential spreads more and more as the atomic number increases. This spreading should cause a lowering of the band-gap energy according to two theories that describe these energy bands: the free-electron theory and the tight-binding approximation theory (Nag, 1995).
The Fourier coefficient for the periodic potential should decrease as the overlapping of the atomic potentials increases, and therefore, the band-gap energy should decrease, according to the free-electron theory. However, increasing overlap should cause a larger coupling between neighboring atoms and a broadening of the allowed band, consequently leading to a narrowing of the forbidden band or a decrease of the band-gap energy (Zhang et al., 2011). When the dispersion of the top valence bands fluctuates within a small energy region, these relatively heavy bands with large effective mass contribute to a high thermopower. For materials with simple band structures, the absolute thermopower value $\alpha$ can be described as follows:

$$\alpha = C \left( \frac{K_B}{e} \right) \ln\left( \frac{\pi m^* K_B T}{n h^3} \right)^{1/2}$$  \hspace{1cm} (2-4)

where $\alpha$ is the thermopower, $K_B$ is the Boltzmann constant, $e$ is the elementary charge, $n$ is the carrier density, $h$ is Planck’s constant, $m^*$ is the effective mass of the charge carrier, $C$ is an integration constant, and $T$ is the absolute temperature (Zhang et al., 2011). Ramdas et al. (Ramdas et al., 2005) investigated the electronic band gaps of semiconductors as influenced by their isotopic composition, and they reported that isotopically controlled crystals offer an extraordinary opportunity to test theoretical predictions using a variety of spectroscopic techniques.
**Table 2.2:** List of some semiconducting elements and compounds together with their bandgaps at 300 K.

<table>
<thead>
<tr>
<th>Material</th>
<th>Direct / Indirect Bandgap</th>
<th>Band Gap Energy at 300 K (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Elements</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C (diamond)</td>
<td>Indirect</td>
<td>5.47</td>
</tr>
<tr>
<td>Ge</td>
<td>Indirect</td>
<td>0.66</td>
</tr>
<tr>
<td>Si</td>
<td>Indirect</td>
<td>1.12</td>
</tr>
<tr>
<td>Sn</td>
<td>Direct</td>
<td>0.08</td>
</tr>
<tr>
<td><strong>Groups III-V compounds</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GaAs</td>
<td>Direct</td>
<td>1.42</td>
</tr>
<tr>
<td>InAs</td>
<td>Direct</td>
<td>0.36</td>
</tr>
<tr>
<td>InSb</td>
<td>Direct</td>
<td>0.17</td>
</tr>
<tr>
<td>GaP</td>
<td>Indirect</td>
<td>2.26</td>
</tr>
<tr>
<td>GaN</td>
<td>Direct</td>
<td>3.36</td>
</tr>
<tr>
<td>InN</td>
<td>Direct</td>
<td>0.70</td>
</tr>
<tr>
<td><strong>Groups III-V compounds</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>α-SiC</td>
<td>Indirect</td>
<td>2.99</td>
</tr>
<tr>
<td>ZnO</td>
<td>Direct</td>
<td>3.35</td>
</tr>
<tr>
<td>CdSe</td>
<td>Direct</td>
<td>1.70</td>
</tr>
<tr>
<td>ZnS</td>
<td>Direct</td>
<td>3.68</td>
</tr>
</tbody>
</table>

(Hummel, 2011)

2.4.2 Charge carrier concentration

An effective adjustment in the carrier concentration dominates the electronic transport behavior by exerting a significant effect on both the electrical conductivity and the Seebeck coefficient (Tan et al., 2012). Furthermore, all thermoelectric properties depend closely on the carrier concentration and typical thermoelectric materials exhibit an optimum carrier concentration of $10^{19} - 10^{21}$ per cm$^3$ (Wang et al., 2011). One of the technologically simplest (and therefore virtually universally used) methods of improving
the thermoelectric properties of a semiconductor material is to choose the optimum level of doping, where `optimum' is used in the sense of maximizing the thermoelectric figure of merit. As mentioned above, an optimum electron concentration exists because, as the concentration increases, the conductivity usually increases, accompanied by a simultaneous decrease in the thermopower (Dmitriev & Zvyagin, 2010). Delaizir et al. (2012) investigated the p-type alloys Bi$_{1-x}$Sb$_x$Te$_3$ with $0.9 \leq x \leq 1.7$, and they observed a linear relation between the amount of antimony, $x$, and the charge-carrier concentration. The thermoelectric properties and non-stoichiometry of GaGeTe have been studied by Drasar et al. (2012), and the authors reported that the measurement of the transport parameters qualitatively indicated that both Ga$_{1+x}$Ge$_{1-x}$Te and GaGeTe$_{1-y}$ are p-type semiconductors ($n \approx 10^{19}$ cm$^{-3}$). Their hole concentration generally rises with increasing $x$ and $y$, as demonstrated by the experiment. However, the negative Seebeck coefficient indicates that the transport processes are dominated by electrons as carriers (Roudebush et al., 2011). Thus, the Seebeck coefficient, the electrical conductivity, and the thermal conductivity vary systematically with the carrier concentration (Anno et al., 2012).

2.4.3 Mobility

In the presence of several scattering mechanisms, theoretical calculation of the resultant mobility of the charge carriers becomes rather complicated. Until now, no thorough analysis of the validity limits of the common theoretical approaches and adopted models has been performed (Mikhnovich Jr., 2001). Electronic transport is described by the (local) electric-field-induced directional velocity component, $\nu$, of the mobile charge carriers (superimposed on their random thermal motion as a time and ensemble average of a fast sequence of acceleration and scattering events), which is associated with a current density $j=e.n.\nu$, where $e$ is the electric unit charge, and $n$ is the local charge-carrier density. The latter can be altered, in principle, by doping, injection, or photo-generation (Karl, 2003). The relation between $\nu$ and the applied electric field $E$ is usually linear for
moderate field strengths (reflecting Ohm’s law), $v = \mu \times E$ and it is obvious that $\mu$, the charge-carrier mobility, is the fundamental (intrinsic) electronic-transport quantity that is specific to a given semiconductor material (Karl, 2003). Because the mobility of electrons serves as a direct relation between the crystal structure and the electrical conductivity, the ratio of the mobility $\mu$ to the thermal conductivity $K$ is a function of the mean atomic weight. Thus, using the relation for mobility in semiconductors and the Pierls relation for thermal conductivity, we can calculate the ratio as a function of the electron mean free path $l_e$ and the phonon mean free path $l_p$ in a crystal (Bulusu & Walker, 2008).

$$
\left( \frac{\mu}{K} \right) = \frac{(4e\rho_m l_e)}{c v_s (2\pi m_e K_B T)^{1/2} l_p}
$$

Here, $\rho_m$ is the mass density; $v_s$ the velocity of sound in the crystal; $c$ is the specific heat of the crystal; and $m_e$ and $e$ are the electron mass and charge, respectively. Using material properties that have been measured for some common semiconductors, the above ratio is plotted against the mean atomic weights of these semiconductors in Figure 2.6.

![Figure 2.6: Ratio of electron mobility to thermal conductivity of thermoelectric materials (Bulusu & Walker, 2008).](image)
2.5 Auxiliary properties

2.5.1 Diffusion properties

Diffusion is the movement of particles from regions of high concentration to regions of low concentration. Diffusion in semiconductors is of great importance for semiconductor technology. As the dimensions of circuits shrink, an understanding of the atom-scale mechanisms of the diffusion processes will become crucial to accurately model and design future devices (Uberuaga et al., 2002). In pure (undoped or unalloyed) compounds, the effects of diffusion are not apparent at temperatures below that at which the compound begins to dissociate (Cadoff & Miller, 1960). Once a small amount of dissociation has taken place, however, the products may diffuse at differing rates in the temperature gradients present in the device, and the diffusion of an intentionally added impurity may exhibit similar behavior, as shown in Figure 2.7. Self-diffusion in binary compound semiconductors is more complex than in elemental semiconductors because of the larger number of possible native point defects that can, in principle, mediate self-diffusion. In addition to vacancies and self-interstitials on the corresponding sublattices, antisite defects must be considered (Bracht et al., 2005). Homogeneities in thermoelectric materials are affected by the temperature gradient because the optimal properties can only be obtained within a very narrow temperature region for each homogeneous material, which greatly limits the efficient utilization of many dispersed energy sources (Cui et al., 2002). However, the diffusion effect depends on the band-gap width and the ratio of electron conductivity to hole conductivity. Heavy carrier doping effectively suppresses the diffusion effect, i.e., it inhibits the increase of thermal conductivity at high temperatures.
Figure 2.7: Effects of diffusion. (a) Unequal rates of diffusion of dissociation products of compound AB results in inhomogeneity. (b) Greater solubility of doping agent C in AB leads to concentration of C at hot end. In both cases, temperature at cold end is insufficient to produce disproportionation (Cadoff & Miller, 1960).

There have been a number of efforts to characterize defect structures by studying defect-structure-sensitive properties, such as impurity diffusion (Nakagawa et al., 2005), and many of these efforts have successfully determined diffusion coefficients in semiconductor materials and have also quantitatively analyzed the diffusion process and predicted the results of annealing. Wanwan et al. (2006) studied the effect of Cd-diffusion annealing on the electrical properties of CdZnTe and reported that the crystal’s resistivity is affected by annealing, which limits diffusion. The nature of this treatment is a diffusion process. Thus, it is meaningful to relate the change in resistivity to the diffusion parameters. The undesirable diffusion of thermoelectric materials when placed in a thermal gradient will result in non-homogeneous and inferior materials, and the importance of diffusion processes is evident at temperatures of approximately 80 percent to 90 percent of the absolute melting point of the materials. A micro-thermoelectric device
consists of a bonding layer, electrodes and thermoelectric thin films. At the interfaces between the metallic electrodes, solder materials and thermoelectric thin films in a micro-thermoelectric device, diffusion occurs and degrades the performance and reliability of the device. Thus, a Ni layer is used as the diffusion barrier in some commercial devices that use bulk thermoelectric materials (Bae et al., 2011). However, because of undesirable and unpredictable diffusion phenomena, modern process technologies try to reduce diffusion by decreasing the thermal range experienced by the device during operation.

2.5.2 Oxidizability

For want of a better term, the tendency of the composition of a thermoelectric material to become altered when exposed to the oxygen in the air may be called “oxidizability.” As is well known, oxygen is a reactive gas. When oxygen is introduced during deposition, highly energetic atomic ions ejected from the target may react with the oxygen ions via collisions and transform into oxides on the target surface. As the oxygen partial pressure increases, the collision probability between the reactive gas and the atomic ions increases, causing the sputtering and deposition rates to decline (Xu et al., 2012). The results of this undesirable phenomenon take two: in one type, a thin surface layer of oxidized material is formed, and the deposition process is inhibited by its formation; the other form involves the diffusion of oxygen into the interior of the material and is therefore progressive (Cadoff & Miller, 1960). Thus far, oxides have been regarded as unsuitable for thermoelectric applications because of their poor mobility, but some years ago, Terasaki (2003) found that a single crystal of the layered cobalt oxide NaCo$_2$O$_4$ exhibits high thermoelectric performance.

Recently, several electrically conductive oxide systems have been recognized as potential candidates for thermoelectric materials; these thermoelectric oxides can be used at high temperatures with no deterioration of their performance caused by oxidation, and
their production costs are comparatively low. Ito and Furumoto (2008); Zhou et al. (2011) investigated the effects of the annealing atmosphere on thermoelectric signals from ZnO films, and they suggested that ambient oxygen plays an important role in the electronic properties of ZnO films. P-type transparent semiconducting oxide (TSO) materials, Cu$_2$O is one of the most promising candidates, and because of the effect of the oxygen flow rate during deposition on the properties of Cu$_2$O films, the oxygen flow rate must be kept low to avoid the over-oxidation of Cu$_2$O to CuO and to ensure a non-oxidized/non-poisoned metallic copper target in the reactive sputtering environment. The proper control of the amount and flow rate of oxygen during deposition can produce good-quality p-type transparent Cu$_2$O films with electrical resistivities ranging from $10^2$ to $10^4$ $\Omega$-cm, hole mobilities of 1–10 cm$^2$/V-s, and optical band gaps of 2.0–2.6 eV (Li et al., 2011). The synthesis and post-annealing effects on the transport properties of thermoelectric oxide (ZnO)$_m$In$_2$O$_3$ ceramics have been studied by Wang et al. (2012), and they inferred that the oxygen defects or vacancies in the InO$_2$ layers play an important role on both the electrical and thermal transport properties of these (ZnO)$_m$In$_2$O$_3$ ceramics. It has also been reported that the resistivity, carrier concentration, and Hall mobility of Z$_5$I$_O$ films depend strongly on the annealing temperature and ambient atmosphere. Measurements of the Seebeck coefficient and electrical resistivity are most likely among the most sensitive means for the detection of small amounts of diffusive oxidation (Cadoff & Miller, 1960). However, in some of the most-studied compounds, traces of diffusive oxidation that are visually and chemically undetectable can so severely affect the Seebeck coefficient as to change its sign, and the resistivity can be increased by several decades as a result of this process.

2.5.3 Brittleness

At low temperatures (T < 200 K), single crystals of the Bi–Sb alloys exhibit the best thermoelectric performances, but the brittleness of the single crystals is a problem in
practical devices. To ameliorate this limitation, some efforts have been devoted to studying the influence of the growth parameters on the mechanical properties of such alloys (Liu et al., 2007). However, the requirements for producing nanostructured TE materials are two-fold: improve their mechanical properties (reduce brittleness and improve machining) and improve their TE properties (figure of merit) (Prokhorov & Pivovarov, 2011). Moon et al. (2010) prepared p-type Te-doped Bi₂Te₃–Sb₂Te₃ compounds using rapid solidification and spark plasma sintering (SPS) techniques, and they reported that the solidified powders consisted of homogeneous thermoelectric phase and that as the SPS temperature increases, the microstructure becomes coarser, resulting in a reduction of the hardness. At present, rapid solidification processes (RSPs) such as gas atomization and melt spinning have been reported to offer a novel opportunity for modifying the intrinsic brittleness and thermoelectric anisotropy of Bi–Te-based thermoelectric materials by forming a fine-grained and homogeneous microstructure (Kim & Chun, 2007). One reason for the broad interest in hardness (H) testing is that the microstructure (and hardness) of materials can change dramatically with alloying, and the machinability of brittle materials also has been correlated with hardness. Thus, the compositional dependence of H is significant because H is related to other mechanical properties. For LAST (lead-antimony-silver-tellurium), the fabrication of thermoelectric (TE) modules for waste-heat recovery will require the machining of perhaps several hundred (or more) individual TE legs. Because machinability and wear resistance are functions of H for other brittle materials (Ren et al., 2008). Zhou et al. (2012) investigated the thermal stability and elastic properties of Mg₂X (X = Si, Ge, Sn, Pb) phases from first-principle calculations and calculated the bulk moduli B, shear moduli G, Young’s moduli E and Poisson ratios ν; they reported that Mg₂Si, Mg₂Ge, Mg₂Sn and Mg₂Pb are all brittle.
2.5.4 Compression and shear strength

The average strength (the mean of the strength distribution) and Young’s modulus (which characterizes the stress–strain response of a brittle material prior to fracture) are fundamental to understanding the mechanical properties of a TE material in a practical device (Fan et al., 2012). Enhancement of the mechanical strength of a TE module will render it more robust. The largest improvement must be in the shear strength, which is the weakest point of many TE modules. The compressive strength also must be increased, especially near the perimeter of the module. Such additional compressive strength will be especially useful in preventing damage to the module if, during the assembly process, clamping forces are accidentally applied unevenly to the module. Not only does the brittleness of the material limit the resistance of the device to mechanical and thermal shocks, but the cutting and fabrication of the arms themselves require that the materials used not be too brittle. Hong et al. (2003) studied the thermoelectric properties of novel n-type 95% Bi₂Te₂ 5% Bi₂Se₃ alloys by gas atomizing and extrusion process, and they reported that the compressive strengths of the compounds hot extruded at 16:1 and 25:1 were 160 and 160 MPa, respectively. The figures of merit $Z$ of the compounds extruded at 16:1 and 25:1 were $2.50 \times 10^{-3}$ K$^{-1}$ and $2.07 \times 10^{-3}$ K$^{-1}$, respectively, because of the different grain sizes induced by the differences in deformation caused by varying the extrusion ratio. The shear strength of aged CoSb₃/Ti/Mo–Cu TE joints has been investigated by Zhao et al. (2009), and the results indicated the joints possessed sufficient strength after aging at 575°C for 720 h. Moreover, the CoSb₃/Ti/W₈₀Cu₂₀ elements exhibit sufficient shear strength and good electrical contact for the reliability of a thermoelectric device (Zhao et al., 2012). Experiments conducted by Zhu and Li (2010) on nanostructured materials, such as nanoparticles, nanowires, nanotubes, nanopillars, thin films, and nanocrystals, have revealed a host of “ultra-strength” phenomena, which are defined by the stresses in a material component generally increasing to a significant fraction (>1/10) of its ideal.
strength – the highest achievable stress of a defect-free crystal at zero temperature. However, while thermoelectric modules exhibit relatively high mechanical strength in the compression mode, their shear strength is comparatively low.

2.5.5 Coefficient of thermal expansion (CTE)

Thermal expansion is critical, as devices for high-temperature applications will be subjected to extreme temperature fluctuations. This property, defined as the fractional change in length or volume with a unit change in temperature, affects several aspects of the design of thermoelectric devices. Generally, the thermal expansion coefficient \( \alpha \) \( (\alpha = (\Delta L/L_0) / (T_2-T_1)) \) varies inversely with the melting temperature \( (T_m) \), and it has been empirically confirmed that the product \( \alpha T_m \) is a constant for many substances. This means that a material with high \( T_m \) should exhibit low \( \alpha \) (D. Y. Jung et al., 2010). The CTE of TE materials is of critical importance because the shear stress is proportional to the temperature gradient, and the larger the heterogeneity in the thermal expansion coefficient of a material is, the larger is the shear stress that will result (Huang et al., 2006). Al-Merbati et al. (2013) examined the influence of device geometry on thermal stress, thermal efficiency and output power, and the result indicated that the presence of high stress can be attributed to the mismatch of thermal expansion coefficients between the pin and the hot plate, which generates high stress levels at the interface between the hot plate and the pin. With respect to the space group (in mathematics and geometry, a space group is a symmetry group, usually for three dimensions, that divides space into discrete repeatable domains), the Pnma phase exhibited a small but significant decrease in thermal expansion with increasing dopant levels, while the Imma phase exhibited no significant change in CTE with increasing dopant levels. However, these values can be considered representative of the behavior of a bulk polycrystalline sample because of the independence of the thermal expansion from microstructure and porosity (Asenath-Smith et al., 2011). Tachibana and Fang (2012) estimated the thermal stress to investigate the
reliability of thermoelectric devices by devices via temperature-cycling tests, and they claimed that it was obvious that the thermal stress was determined by the temperature difference, coefficients of thermal expansion, die height, die cross section, substrate size and so on. However, no explicit relations among these parameters were given. Rogl et al. (2012) investigated the effects of high pressure torsion (HPT) processing on the structural, thermoelectric and mechanical properties of Sr$_{0.07}$Ba$_{0.07}$Yb$_{0.07}$Co$_4$Sb$_{12}$, and they reported that the thermal expansion coefficient below room temperature after processing was slightly lower than before HPT. The thermal expansion of the sample was measured above room temperature both parallel and perpendicular to the pressing direction, and interesting results were obtained: the thermal expansion coefficient calculated for the temperature range of 600–700 K was the same as for the low-temperature region, but the expansion behavior from room temperature to 550 K differed between the first and third measurements and requires further investigation. As the temperature increased from 300 to 550 K, the length first reached a maximum and then was observed to decrease.

2.6 Applications

Thermoelectric (TE) modules comprise arrays of thermoelectric (TE) junctions, which are connected electrically in series and thermally in parallel. The TE junctions, in turn, consist of p- and n-type thermoelectric materials, which are selected from the range of materials discussed so far in this review, based primarily on their physical thermoelectric performance. Auxiliary to the basic array of TE modules are components that contribute to the overall efficiency of the module, such as heat sinks, which absorb heat from the hot side, and cooling fins or cooling systems, which dissipate heat from the cool side. Typically, a single module may produce power in the range of 1 to 125 W and may be modularly connected to produce power up to ~5 kW. The maximum temperature gradient between the hot and cold side can be as high as 70°C (Riffat & Ma, 2003). The general TE module architecture is shown in Figure 2.8. Given the nature of TE modules as solid-
state devices with no moving parts, they are durable and reliable, with over 100,000 hours of operating lifetimes, and have a simple structure. They may operate in two modes: as thermoelectric generators (TEGs), generating electricity from a temperature gradient, or as thermoelectric coolers (TECs), converting a direct current into a temperature gradient (Ahiska et al., 2012).

Figure 2.8: Schematic of atypical thermoelectric device (Saidur et al., 2012).

2.6.1 Applications of thermoelectric devices as coolers

Thermoelectric coolers, which are commonly known as Peltier coolers, have been successfully commercialized for high-performance, niche cooling systems that require high heat-flux dissipation to a very low temperature at a precise rate. These Peltier coolers are well suited for such applications, for which a conventional air-cooling system is no longer adequate to remove the heat fluxes at a sufficiently high rate. The general design criteria for these TECs include high reliability, flexibility in packaging and integration and low weight (Chein & Huang, 2004; Putra et al., 2011).
2.6.1.1 Cooling electronic devices

In electronic cooling applications, a thermoelectric cooler (TEC) serves as a device for transporting heat away from a surface that has a temperature higher than the ambient temperature. The purpose of a TEC is to maintain the junction temperature of an electronic device below a safe temperature by pumping heat away from the device (Chein & Huang, 2004). A significant increase in both microprocessor power dissipation and CPU size has resulted in an increase in heat fluxes. As a result of the increasing miniaturization of electronic circuitry, microprocessor heat fluxes have also increased and are expected to exceed 100 W/cm² for many commercial applications (Putra et al., 2011).

The development of thermoelectric coolers (TECs) in combination with air cooling or liquid cooling approaches has been of major thermal benefit because a negative temperature gradient and, therefore, a reduced thermal resistance can be generated with the use of a TEC. Figure 2.9 illustrates air-cooling techniques (in which a fan is simply added to blow air through the enclosure that houses the electronic components to enhance the heat transfer) for high-power electronic packages such as processors (Zhang et al., 2010).

![Figure 2.9: Schematic of the TEC cooling of a processor with an air cooled heat sink at the top (H. Y. Zhang et al., 2010).](image)

In addition, TEC applications have been studied for hot-spot thermal management. To aid the design and analysis of these TECs, intensive modeling work concerning the
performance of TECs has been carried out, such as that for the material Bi$_2$Te$_3$ (PrezAparicio et al., 2012). Chang et al. (2009) a theoretical model of a thermal analogy network was developed to predict the thermal performance of a TEC with an air-cooling module. They reported that at a specific heat load, the TEC air-cooling module achieves its best cooling performance at an optimum input current between 6 A and 7 A and for heat loads between 20W and 100W. Their result also demonstrated that the thermoelectric air-cooling module performs better at a lower heat load. Similarly, Huang et al. (2010) demonstrated experimentally that the thermal performance of a conventional water-cooling device can be effectively enhanced by integrating it with a thermoelectric cooler when the heat load is below 57 W. Zhou and Yu (2012) conducted detailed analyses of the optimal allocation of the finite thermal conductance between the cold-side and hot-side heat exchangers of a TEC system. The analysis results when the constraint of the total thermal conductance was considered demonstrated that the maximum coefficient of performance (COP) can exceed 1.5 when the finite total thermal conductance is optimally allocated. However, overall, the efficiency of the hot-side heat exchanger parameters is usually the predominant factor in determining the overall performance of a TEC system (Wang et al., 2013; Zhou & Yu, 2012).

2.6.1.2 Refrigerators and air conditioners

In refrigeration applications for which cost is not the main criterion, Peltier cooling appliances provide rapid cooling; a solar Peltier refrigerator may reduce the temperature from 27°C to 5°C in approximately 44 min (Abdul-Wahab et al., 2009). A thermoelectric refrigeration system, which has the merits of being light, reliable, noiseless, rugged, and low cost in mass production, uses the charge carriers in the thermoelectric material rather than refrigerant as the heat dissipation carrier (Dai et al., 2003). One attractive application is for outdoor purposes, when operated in tandem with solar cells, as shown in Figure 2.10. In the daytime, solar cells receive solar energy and turn it into electric power
supplied to the thermoelectric refrigerator by means of the photovoltaic effect. If the amount of electric power produced is sufficient, the power surplus can be accumulated in a storage battery in addition to driving the refrigerator. If the solar cells cannot produce sufficient electric power, for example, on cloudy or rainy days, the storage battery may serve as a supplementary power source, and it can be used to power the refrigerator at night. Although the coefficient of performance of such a system is not as high as for a vapor-compression cycle (Dai et al., 2003), thermoelectric refrigerators have been used in military, aerospace, instrument, and industrial or commercial products as cooling devices for specific purposes; for example, TEC systems, when used as microclimate cooling (MCC) systems, can remove a significant amount of heat from a soldier's body while he or she is wearing combat clothing, thus increasing mission duration and enhancing mission performance (Chen et al., 2012). Luo et al. (2013) investigated the cooling potential of bulk single-phase Bi$_{85}$Sb$_{15}$ material. This material, which was prepared via melt spinning (MS) combined with a subsequent spark plasma sintering (SPS) technique, provided an optimized power factor of 7.9 mW/mK$^2$ for the sample with the highest cooling rate. Meng et al. (2011) conducted numerical studies of the cooling load and coefficient of performance of a commercial water-cooling thermoelectric refrigerator with a maximum cooling load of 2.33 W and a maximum COP of 0.54. The results demonstrated that the heat convection of the heat exchanger and the heat leakage through the air gap are the main factors that can cause irreversibility and decrease the performance of the system. The COPs of present commercial thermoelectric refrigerators (for example, Melcor’s Polar TECTM series of thermoelectric devices) are typically between 0.3 and 0.7 for single-stage applications. Moreover, COPs greater than 1.0 can be achieved when the module is removing heat from an object that is warmer than the ambient temperature (TE Technology, 2010).
Figure 2.10: Schematic of solar cell driven, thermoelectric refrigerator (prototype) (Dai et al., 2003).

Thermoelectric air conditioners (TEACs) are environmentally friendly, simple and reliable; they offer convenient installation and support complex water distribution pipes, and switching between the cooling and heating modes can be easily achieved by reversing the input current. However, these systems are still very expensive at present (Shen et al., 2013). TEACs are portable and low noise, but they have a relatively low COP, which is an additional factor that limits their application for domestic cooling. TEACs, however, have a large potential market as air conditioners for small enclosures, such as cars and submarine cabins, where the power consumption would be low or safety and reliability would be important (Riffat & Qiu, 2004). For example, Cherkez (2012) theoretically determined the maximum coefficient of performance (COP) of an air conditioner based on a permeable thermoelectric converter. Considering the optimal structural and thermophysical parameters, including the applied electrical current and the heat-carrier
velocity in the channels of the thermo-elements, the results indicated the possibility of increasing the COP by a factor of 1.6 - 1.7.

2.6.2 Application of thermoelectric devices for power generation

Thermoelectric generators (TEG), in principle, may offer many advantages over conventional electric-power generators, such as being highly reliable, silent in operation, and environmentally friendly and containing no moving parts (Niu et al., 2009). Because of these advantages, considerable emphasis has been placed on the development of TEGs as a standalone power-generation technology for a variety of aerospace, biomedical, remote power and military applications (Riffat & Ma, 2003).

2.6.2.1 Low power generation

Body-mounted electronic devices may be broadly categorized into those intended for mobile communications purposes, such as smartphones, MP3 players and iPods, and those for medical purposes, such as hearing aids and cardiac pacemakers. The power requirements of these body-mounted devices range from 5 μW to 1 W, with a corresponding life expectancy of up to 5 years, indicating a need for an energy source that is both portable and autonomous (Vullers et al., 2009). Today, batteries represent the dominant energy source for portable devices. Although the energy density of batteries has increased by a factor of 3 over the past 15 years, in many cases, their presence has had a large impact on, or even dominated, the overall size and operational cost of portable devices (Vullers et al., 2009). Furthermore, batteries contain chemical substances or materials that are harmful to the environment, such as sulfuric acid, mercury, zinc, lithium, lead, nickel and cadmium, and exhibit toxicity that can cause damage to humans and the environment. For this reason, body-mounted TEGs are an attractive proposition, as they may be fabricated out of safer materials than Ni-Cd or lithium-ion batteries (Riffat & Ma, 2003). So far, a thermoelectric wristwatch that is driven by body heat has appeared
as one commercialized example of body-mounted TEGs. Two known manufacturers of these TEG wristwatches are Seiko and Citizen; the Seiko watch typically produces 300 mV of open-circuit voltage from a temperature gradient of 1.5 K, and its efficiency is approximately 0.1% (Snyder, Fall 2008).

2.6.2.2 High power generation

(a) Waste heat thermoelectric generators

Traditionally, large-scale electricity generation is achieved via the burning of fossil fuels (e.g., heat engines) or from nuclear or hydropower sources. Each of these technologies has some disadvantages in terms of environmental impact. For example, the burning of fossil fuels has been linked to environmental pollution and global warming, while nuclear electricity carries a risk of nuclear meltdown, as demonstrated by the 2011 Fukushima disaster. TEGs circumvent these problems, as they generally offer a low environmental risk. Furthermore, TEGs are an intelligent way of mitigating the adverse effects of global warming, as they are able to generate electricity by harvesting waste heat, such as heat that is the byproduct of industrial processes, such as the steelworks industry, and automobile engines. Recognizing the potential of waste heat as an energy resource, these two industries have been the main driving force behind the development of commercial TEGs for high-power electricity generation. The energy-conversion efficiency of a TEG ($\eta_{\text{ee}}$) is determined by both the operating temperature of the generator and the unitless figures of merit ($ZT$) of the thermoelectric materials used, as follows:

$$\eta_{\text{ee}} = \left(\frac{T_h - T_c}{T_h}\right) \left(\frac{\sqrt{(1 + ZT)} - 1}{\sqrt{(1 + ZT)} + \frac{T_c}{T_h}}\right)$$

2-6

where $T_h$ is the hot-side temperature, and $T_c$ is the cold-side temperature; these temperatures are selected based on the application of the TEG. Komatsu’s Bi$_2$Te$_3$-based
thermoelectric generator, touted as the world’s most efficient, has $\eta = 7.2\%$ and produces an output density of approximately 1 W/cm$^2$ when operating at $T_c = 30^\circ$C and $T_h = 280^\circ$C (Group, 2010). In the case of waste-heat-recovery power generation, several leading automobile manufacturers, such as Volkswagen, Volvo, Ford and BMW, have been developing TEG waste-heat-recovery systems to improve the fuel economy of their automobiles with potential power generated from the TEGs in the range of ~1 kW. Even despite the currently low TEG efficiency, diligent harvesting of waste heat from resources such as automobile exhaust via judicious design and fabrication methods and maintenance strategies render TEGs a worthwhile technology for investment by these automobile manufacturers (Snyder, Fall 2008). A TEG with a $ZT$ of 1.25 and an efficiency of approximately 10% could be used to harvest 35% to 40% of the energy from the exhaust manifold, which has an average temperature of 250°C, to generate useable power that would contribute directly to the operation of the equipped vehicle, which could increase fuel efficiency by up to 16% (Yu & Chau, 2009). Most of these automobile TEGs use BiTe-based bulk thermoelectric materials, as an optimal $ZT$ in the temperature range < 500 K may be achieved using this compound, and therefore, the manufacturing processes for this compound have been extensively developed. Table 2.3 presents the characteristics of available thermoelectric generator semiconductors (Tie & Tan, 2013). Hsu et al. (2011) have designed a system for the recovery of waste heat that comprises 24 TEG modules to convert heat from the exhaust pipe of an automobile to electrical power; a temperature difference of 30 °C was able to produce a total power output of 12.41 W. In another development effort, Karri et al. (2011) simulated a performance comparison of a TEG containing bismuth telluride (Bi$_2$Te$_3$) and quantum-well (QW) thermoelectric materials. The TEGs containing these two materials were placed in the exhaust streams of a sports utility vehicle (SUV) and a stationary, compressed-natural-gas-fueled engine generator set (CNG). The results predicted an increase in power between the QW- and
Bi$_2$Te$_3$-based generators of approximately a factor of three for the SUV and a factor of seven for the CNG generator under the same simulation conditions. The relative fuel savings for the SUV averaged approximately -0.2% using Bi$_2$Te$_3$ and 1.25% using the QW generator. For the CNG case, the fuel savings was approximately 0.4% using Bi$_2$Te$_3$ and approximately 3% using the QW generator. However, any temperature fluctuation on the hot side leads to a rapid change in the output power generated by the TEG, which is dangerous to electric devices (Gou et al., 2013).

Table 2.3: The characteristic of available thermoelectric generator materials.

<table>
<thead>
<tr>
<th>Temperature (°C)</th>
<th>Type</th>
<th>TEG materials</th>
<th>ZT (maximum)</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt; 150</td>
<td>p</td>
<td>Bi$_2$Te$_3$</td>
<td>0.8</td>
</tr>
<tr>
<td></td>
<td>n</td>
<td>Bi$_2$Te$_3$</td>
<td>0.8</td>
</tr>
<tr>
<td>150 - 500</td>
<td>p</td>
<td>Zn$_4$Sb$_3$</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>p, n</td>
<td>PbTe</td>
<td>0.7 – 0.8</td>
</tr>
<tr>
<td></td>
<td>p</td>
<td>TeAgGeSb(TAGS)</td>
<td>1.2</td>
</tr>
<tr>
<td>500 - 700</td>
<td>p</td>
<td>CeFe$<em>4$Sb$</em>{12}$</td>
<td>1.1</td>
</tr>
<tr>
<td></td>
<td>n</td>
<td>CoSb$_3$</td>
<td>0.8</td>
</tr>
<tr>
<td>700- 900</td>
<td>p, n</td>
<td>SiGe</td>
<td>0.6 – 1.0</td>
</tr>
<tr>
<td></td>
<td>p</td>
<td>LaTe</td>
<td>0.4</td>
</tr>
</tbody>
</table>

(Tie & Tan, 2013)

While the energy conversion efficiency is a useful metric for considering the performance and selection of TEGs, the cost of generating electricity is of comparatively equal importance for the development of commercial devices. For practical applications, the cost of power generation – as governed by material, manufacturing, and heat-exchanger costs – is a critical factor that is not captured by the figure of merit, $ZT$, alone (Yee et al., 2013). Komatsu, which boasts the world’s highest-efficiency TEG module, in
their technical report by Sano et al. (2003), deduced that the selling prices of Bi-Te-based thermoelectric modules range from $7 to $42 per watt at a maximum energy-conversion efficiency of 15%. Consequently, current applications of TEGs are restricted to niche sectors where reliable power generation is required irrespective of cost and efficiency, such as deep-space missions and oil and gas platforms.

(b) Solar thermoelectric generators (STEGs)

Solar thermoelectric generators (STEGs) were initially designed and optimized for space applications because of their advantages of reliability and long lifetimes as well as their ability to capture high levels of incident solar radiation in extraterrestrial regions; however, much of the recent interest in these systems has been focused on residential solar-thermal-energy harvesting (Deng et al., 2013; He et al., 2012; Kraemer et al., 2012; Omer & Infield, 1998, 2000; Suter et al., 2010; Xi et al., 2007, Xiao et al., 2012). The STEG may be described as consisting of a TEG and a thermal collector. Solar heat can be absorbed by the thermal collector and then concentrated and conducted over the thermoelectric generator using a fluid pipe or some other means. Subsequently, the thermal resistance of the thermoelectric generator will lead to a temperature difference that is proportional to the heat flux from the absorber of the thermal collector to the fluid. As a result, electric power will be generated by the thermoelectric generator, and this power will be proportional to the temperature difference (Xi et al., 2007). Suter et al. (2010) simulated a 4-leg TEC module consisting of two pairs of p-type La$_{1.98}$Sr$_{0.02}$CuO$_4$ and n-type CaMn$_{0.98}$Nb$_{0.02}$O$_3$ legs sandwiched between two ceramic Al$_2$O$_3$ hot/cold plates and exposed to concentrated solar radiation. The heat-transfer analysis for the module indicated that a large amount of solar heat is lost in such STEGs: more than 70% of the incident solar power was lost to re-radiation and free convection from the absorber, while 20% was conducted through the legs, and <10% was lost via radiation to the cold plate, resulting in a maximum efficiency of only 0.081%. Further experimental and analytical
improvements to overcome these thermal losses were achieved by He et al. (2012), who incorporated thermoelectric modules with glass evacuated-tube heat-pipe solar collectors (SHP-TE). The simulation results indicated that the evacuated-tube heat-pipe solar collectors had a significant effect on the TEG by increasing the thermal efficiency by approximately 55%, which may increase the performance to above 1%. Meanwhile, Kraemer et al. (2012) predicted a peak efficiency of 5 with a thermoelectric material cost of below 0.05 $/W, by modeling an optimized methodology for terrestrial solar thermoelectric generators (STEGs). Miljkovic and Wang (2011) modeled and optimized a novel hybrid solar thermoelectric (HSTE) system that uses a thermosyphon to passively transfer heat to a bottoming cycle to determine the overall performance in a temperature range of 300–1200 K for solar concentrations of 1–100 suns and various thermosyphon and thermoelectric materials with a geometry resembling an evacuated-tube solar collector. Bismuth telluride, lead telluride, and silicon germanium thermoelectrics were studied with copper/water, stainless-steel/mercury, and nickel/liquid-potassium thermosyphon/working-fluid combinations. The system contained a parabolic trough mirror that concentrated solar energy onto a selective-surface-coated thermoelectric to generate electrical power, and a thermosyphon adjacent to the back side of the thermoelectric maintained the temperature of the cold junction and carried the remaining thermal energy to a bottoming cycle; see Figure 2.11. This HSTE system demonstrated that ideal efficiencies as high as 52.6% can be achieved at a solar concentration of 100 suns and a bottoming-cycle temperature of 776 K. However, the performance of a solar thermoelectric generator is primarily limited by the thermoelectric materials used to construct it; bismuth telluride is a favorable low-temperature thermoelectric material that exhibits advantageous properties and can reaches a maximum of $ZT \sim 1$ at low temperatures in the range of (25–225°C), while filled skutterudite is a good medium-temperature thermoelectric material that can be operated over a wide temperature range.
Moreover, the total conversion efficiency for solar energy of a solar thermoelectric generator based on a multi-stage thermoelectric module could be as high as 10%. With the continuous emergence of new thermoelectric materials, solar thermoelectric generators using multi-stage and hybrid-generation-system (HGS) thermoelectric modules will have good application prospects (Deng et al., 2013; Xiao et al., 2012).

![Figure 2.11: Schematic of the hybrid solar thermoelectric system (HSTE).](image)

**Figure 2.11:** Schematic of the hybrid solar thermoelectric system (HSTE). (Miljkovic & Wang, 2011).

### 2.6.3 Applications of thermoelectric devices as thermal-energy sensors

Many new types of thermal-energy sensors based on the Peltier effect or Seebeck effect of thermoelectric modules have been developed in the last two decades, such as sensors for power ultrasound effects (Faid et al., 1998), cryogenic heat-flux sensors (Ahamat & Tierney, 2011; Faid et al., 1998), water-condensation detectors (Sawaguchi et al., 2005; Vancauwenberghe et al., 1996), fluid-flow sensors (Jacobs, Kutzner, Kropp, Brokmann, et al., 2009; Jacobs, Kutzner, Kropp, Lang, et al., 2009; Stachowiak et al., 1998), and infrared sensors (Escriba et al., 2005; Hirota et al., 2007; Ihring et al., 2011; Müller et
These sensors generally rely on the conversion of heat into electrical signals or vice versa.

Infrared (IR) sensors, which operate on the principle that any mass radiates heat, allow the detection of heat using the Seebeck effect; the absorption of heat causes a specific temperature rise, which subsequently produces a Seebeck voltage. The main sensor parameters are the responsivity, which is given by the ratio of the sensor voltage to the incoming radiation power; the time constant; and the noise voltage (Escriba et al., 2005; Müller et al., 1996). Hirota et al. (2007) developed a low-cost thermoelectric infrared sensor (thermopile) using polysilicon with a precisely patterned Au-black absorber that provides a high responsivity of 3900 V/W and a low cost potential. However, most thermoelectric IR sensors are able to operate in the range of 7 to 14 μm.

Kopparthy et al. (2012) developed a thermoelectric microfluidic sensor (TMS) for biochemical applications. The device consists of a 100 μm deep microfluidic channel with a Bi/Sb thin-film thermopile attached to its bottom surface. The device has a sensitivity of 0.045 V-s J⁻¹ when known quantities of energy are applied to a nichrome heater incorporated on the inner side of the bottom wall of the microfluidic sensor bottom channel wall, while continuously injecting deionized (DI) water. Using the Seebeck and Peltier effects Stachowiak et al. (1998) developed a fluid-flow sensor for use in the low-velocity range. This sensor, when placed in a typical cylindrical duct of 100 mm in diameter, produced an output signal of 185 μV for a fluid-flow range from zero to 1.5 m³/s with a maximum error of ± 4%. A sensor system combining a novel pressure-stable thermoelectric flow and an impedimetric sensor for monitoring chemical conversion in microfluidic channels was developed by Jacobs et al. (2009). Both sensor chips were optimized for hydraulic diameters of ~1 mm and exhibit a high chemical, temperature and
pressure stability. However, in terms of size and light weight, the most effective structure for thermoelectric sensors is the thin-film structure (Kozlov, 1999, 2000).

2.6.4 Aerospace applications

Advanced autonomous power systems that can be operated continuously and independently of the sun and are capable of providing electric power from a few watts to hundreds of kilowatts for 7–10 years are required for extraterrestrial exploration vehicles. For example, the solar brightness on Mars and Jupiter is as weak as 45% and 4%, respectively, and it is negligible on other planets. As a result, the solar option is suitable only for robotic and spacecraft missions that are limited in their time scope of operation and require only a few watts of electrical power (~10 W) (El-Genk & Saber, 2005).

Radioisotope thermoelectric generators (RTGs) have been used by the United States to provide electrical power for spacecraft since 1961. The required electrical output power levels can be achieved by the appropriate selection of a number of general-purpose heat-source (GPHS) modules incorporated in an RTG system. A GPHS module is a composite carbon body that houses a total of four fuel pellets and acts as an aero-impact shell. The isotope fuel for the GPHS-RTG is in the form of plutonium dioxide ($^{238}\text{PuO}_2$) at approximately 80% density. For power conversion by the GPHS-RTG, thermoelectric junctions have been used, such as SiGe junctions (O’Brien et al., 2008). SiGe unicouples partially convert the heat generated by the radioactive decay of $^{238}\text{Pu}$ in the $^{238}\text{PuO}_2$ fuel pellets that are encapsulated in the general-purpose heat-source (GPHS) modules (El-Genk et al., 2003), as shown in Figure 2.12. Previously, lead telluride was used as the thermoelectric converter for lower-powered RTGs operated at a maximum hot junction temperature of <865 K to produce a power of ~2.7 W (Rinehart, 2001). Because of the deleterious effects of oxygen on these materials (Lange & Carroll, 2008), silicon-germanium thermoelectric elements were later adopted for high-powered RTGs operated at high temperatures of up to 1275 K (Rinehart, 2001). Their sublimation rates and
oxidation effects, even at these higher temperatures, can be controlled by the use of sublimation barriers around the elements and an inert cover gas within the generator during ground operation (Lange & Carroll, 2008). In 1976, the Lincoln Experimental Satellite (LES) 8/9 was the first spacecraft to use the new ">150 \text{ W}_e\) multi-hundred watt (MHW) RTG," which employed 312 SiGe-alloy thermoelectric elements per RTG (Bennett et al., 1996).

**Figure 2.12:** Current RTGs with 18 GPHS modules and SiGe thermoelectric unicouples for generating 280 \text{ W}_e\) at beginning of life (~5.5 \text{ W}_e/\text{kg}) (El-Genk et al., 2003).

Recently, skutterudite alloys with ZTs ranging from ~0.92 to 1.48 in the temperature range from 300 to 973 K (El-Genk et al., 2003) have been developed at the Jet Propulsion Laboratory (JPL) in Pasadena, California and are being considered for use in Advanced Radioisotope Power Systems (ARPSs) to support NASA’s planetary exploration missions (El-Genk et al., 2006). The use of skutterudite unicouples in the bottom array with SiGe unicouples in the top array has been proposed for cascaded thermoelectric modules (CTMs) for use in radioisotope power systems (RPSs) to generate electric power of 108 \text{ W}_e\) and to achieve a net decrease of ~43\% in the required amount of $^{238}$PuO$_2$ (El-Genk & Saber, 2006). However, an operational issue with skutterudite-based unicouples is the sublimation of antimony from the legs near the hot junction at ~973 K. Such sublimation
could change the thermoelectric properties of the material and degrade the unicouples’ performance over time (El-Genk et al., 2006). The use of TEGs in commercial aerospace vehicles, which is expected to reduce fuel consumption by 0.5%, is also being explored by Boeing Research & Technology (Huang, 2009). As a rough estimate, this fuel savings, if implemented solely in the US, would save passenger and cargo airlines more than $12 million every month and reduce global carbon emissions by 0.03% (Kousksou et al., 2011).
3.1 Synthesis of skutterudite materials

In this research, CoSb\(_3\) skutterudite voids were filled with transition metals such as Mn and Hf, as well as other metals such as Al, to form ternary skutterudites. This strategy is a departure from the conventional approach of substituting Co atoms in skutterudites, as attempted by Kitagawa et al. (2005) and Ur et al. (2007) using Ni and Fe in the CoSb\(_3\) matrix. Next, the effect of excess doping on the texture of the grain boundaries in enhancing thermoelectric performance was assessed through Al addition.

Ternary skutterudite formulations were then investigated with lanthanide (Yb) acting as a partial filler for CoSb\(_3\) skutterudite. In this work, doping of Al and Bi was attempted to modify grain boundaries to achieve superior thermoelectric performance. The particle size and purity of the elements used in the synthesis and the atomic ratio of the formulations are shown in Table 3.1. The synthesis and characterization of the skutterudite materials included two preparation steps and several properties, which are shown in the flowchart of Figure 3.1.

**Table 3.1:** The elements used in the synthesis and the atomic ratio of the formulations

<table>
<thead>
<tr>
<th>Materials</th>
<th>Formulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elemental Powders</td>
<td>Mn (200 mesh, &gt;99.9 wt%), Hf (200 mesh, &gt;99.9 wt%), Al (200 mesh, &gt;99.99 wt%), Bi (200 mesh, &gt;99.9 wt%), Yb (200 mesh, &gt;99.9 wt%), Co (22 mesh, &gt;99.998 wt%) and Sb (200 mesh, &gt;99.99 wt%)</td>
</tr>
<tr>
<td>Ternary Skutterudites</td>
<td>(1Mn:4Co:12Sb), (1Hf:4Co:12Sb), (0.3Al:4Co:12Sb), (0.6Al:4Co:12Sb), and (2Al:4Co:12Sb)</td>
</tr>
<tr>
<td>Quaternary Skutterudites</td>
<td>(0.1Al:0.25Yb:4Co:12Sb), (0.2Al:0.25Yb:4Co:12Sb), (0.3Al:0.25Yb:4Co:12Sb), and (0.1Bi:0.25Yb:4Co:12Sb)</td>
</tr>
<tr>
<td>Quintuple Skutterudites</td>
<td>(0.1Al:0.05Bi:0.25Yb:4Co:12Sb)</td>
</tr>
</tbody>
</table>
Figure 3.1: Flowchart of sample preparation and characterizations.
3.1.1 Mechanical alloying technique

The mixed powders were subjected to mechanical alloying in a planetary ball mill (GOKIN Ltd., PLANET) with a milling time of 10 h. Zirconium oxide vials and balls (φ=5 mm) were used. The ball-to-powder weight ratio was maintained at 15:1. The rotation speed was fixed at 400 rpm. To avoid contamination and oxidization, the powders were loaded and unloaded in a glove box filled with an argon atmosphere.

3.1.2 Spark plasma sintering process

Using the spark plasma sintering (SPS) system shown in Figure 3.2(a), the powders pretreated by MA were pressed under a vacuum atmosphere in a cylindrical die with an inner diameter of 10 mm that was lined with graphite sheet to facilitate easy removal of the sintered compact. The sintering process was performed under a uniaxial press static pressure of 36 MPa combined with a pulsed DC power supply via the graphite die. A heating rate of 100 °C min⁻¹ from room temperature to 600 °C was used. The temperature was then held at 600 °C for 10 min, after which the sample was left to cool naturally for 2 hours. Temperature control during the SPS process was carried out using a K-type thermocouple located in a hole that had been drilled into the graphite die up to 1 mm to the sample/die interface (see Figure 3.2(b)). The actual temperature distribution within the powder sample, which depends on the sample material’s electrical conductivity and the die wall thickness and material, can deviate from the measured temperature, and thus only an ‘apparent’ temperature is recorded by this method. Finally, the disc sample obtained from the SPS process was extracted from the die and manually ground (see Figure 3.2(c)) to remove the remaining graphite sheet stuck to the sample surface from the process. Silicon carbide (SiC) sandpaper was used to grind the samples. The SiC sandpaper was selected by grit size in a sequence of 800, 1200, 2400, and 4000; the grit is the number of grains of silicon carbide per square inch of abrasive paper.
3.2 Microstructural analysis

3.2.1 X-ray powder diffraction

In this study, X-ray diffraction (XRD) was used to elucidate structural information of the disc samples using the Bruker AXS D8 Advance X-ray diffraction spectrometer shown in Figure 3.3 with Cu-Kα at a wavelength of 1.5406 Å. The patterns were recorded in a 2θ range between 10° and 90° at a rate of 0.0264 in step width. The lattice parameters of the compound were calculated using the following formulae:

\[ \frac{1}{d^2} = \frac{h^2}{a^2} + \frac{k^2}{b^2} + \frac{l^2}{c^2} \quad \text{and} \quad d = \frac{\lambda}{2 \sin \theta} \]

3-1

The scattered waves produced a unique pattern corresponding to the compositions of the sample, and comparative analysis was therefore performed using HighScore Plus.
software to determine the chemical composition of the samples from their recorded patterns.

Figure 3.3: Bruker AXS D8 Advance X-ray Diffraction spectrometer.

3.2.2 Scanning electron microscopy

The samples were subsequently ground and polished with a “Struers TegraPol-21” machine. Silicon carbide (SiC) sandpaper was used to grind the samples. The SiC sandpaper was selected by grit size in a sequence of 800, 1200, 2400, and 4000. The rotation direction of the sample holder was contrary to the direction of the grinding disc rotation. The duration with each grit size was 1 min under 15 N of force at a disk speed
of 150 rpm. Tap water was used for lubrication during grinding by the SiC sandpaper. The specimens and holding disk of the grinding machine were washed and dried after each use to prevent contamination from larger grit sizes. After grinding with the 4000 SiC sandpaper, the polishing process began with a polycrystalline diamond suspension as the abrasive (particle size: 3.0 μm) on a MD-MOL polishing cloth. Final polishing was performed with a MD-CHEM polishing cloth using a colloidal silica suspension (particle size: 0.04 μm). After polishing, the sample surface was thoroughly cleaned with distilled water and methyl alcohol and dried with a hot air blower to eliminate water spots and to remove any remaining residue.

Scanning electron microscopy was used to observe the specimen surfaces. When the specimen is irradiated with a fine electron beam (called an electron probe), secondary electrons are emitted from the specimen surface. The topography of the surface can be observed by two-dimensional scanning of the electron probe over the surface and acquisition of an image from the detected secondary electrons. The SEM instrument contains an electron optical system to produce an electron probe, a specimen stage to support the specimen, a secondary electron detector to collect secondary electrons, an image display unit, and an operation system to perform various operations.

The FEI Helios 450HP dual beam linked with energy-dispersive X-ray spectroscopy (EDX) shown in Figure 3.4 was used for imaging, structure determination and elemental mapping. The FEI Helios NanoLab 650 dual beam is a state-of-the-art scanning electron microscope (SEM) and a focused ion beam (FIB) packaged in one instrument, designed for extremely high-resolution 2D and 3D characterization, nanoprotopyping, and sample preparation. The incredible versatility of this machine accommodates conventional imaging and analysis in addition to site-specific analysis, deposition, and ablation of materials with the ion beam. In this system, the SEM is configured to provide complete
analysis of the samples. This includes true surface imaging, atomic number imaging, elemental analysis (energy dispersive X-ray spectroscopy), and crystal orientation (electron backscattered diffraction).

In this study, the FIB was used for high-resolution imaging and real phase structure determination. In addition, because the main purpose of this source is sample preparation, the FIB was used to remove materials for the preparation of electron transparent lamellae for subsequent scanning transmission electron microscopy.

**Figure 3.4:** FEI Helios 450HP DualBeam FIB-SEM.

### 3.2.3 Transmission electron microscopy

After the electron transparent lamellae was prepared by FIB, the transmission electron microscope (TEM), model Tecnai G2 F20 from FEI, shown in Figure 3.5 was used to investigate the nano-scale structure. The system was linked to an Oxford instruments EDS detector, which was used for the elemental mapping and determination of the chemical
compositions. The main features of this setup are as follows: ZrO2/W (100) Schottky field emitter (FEG); twin objective lens; point resolution: 0.27 nm; information limit: 0.16 nm; magnification range: 21x - 700 kx in TEM mode and 410x - 1350 kx in EFTEM mode; camera length range: 52 – 1500 mm in TEM mode and 110 – 7000 mm in EFTEM mode; fully computer-controlled; eucentric side-entry; high-stability CompuStage; Gatan Tridiem GIF-CCD: 2kx2k CCD camera and post column energy filter (GIF); Fischione ultra-high resolution STEM HAADF detector; single and double tilt specimen holders ($\alpha = +/- 60^\circ$); Gatan 626 cryo specimen holder, cryo transfer station and cold stage controller; FEI Vitrobot for cryo-TEM preparation; Xplore3D for automated tomographic tilt series acquisition; and Inspect 3D on a support PC for tomographic reconstructions.

**Figure 3.5:** Transmission electron microscope (TEM) from FEI (model: Tecnai G2 F20)
3.2.4 X-ray Photoelectron Spectroscopy

The X-ray photoelectron spectroscopy (XPS) instrument from Ulvac Phi (model: Quanterra II) shown in Figure 3.6, also known as electron spectroscopy for chemical analysis (ESCA), was used in this work to provide quantitative and chemical state information from the surface of the material being studied. The PHI XPS instrument provided the ability to obtain spectra with a lateral spatial resolution as small as 7.5 µm, with an average depth of analysis of approximately 5 nm. Spatial distribution information was obtained by scanning the micro focused X-ray beam across the sample surface. XPS was typically accomplished by exciting the sample surface with mono-energetic Al kα X-rays, causing photoelectrons to be emitted from the sample surface. An electron energy analyzer was used to measure the energy of the emitted photoelectrons. From the binding energy and intensity of a photoelectron peak, the elemental identity, chemical state, and quantity of a detected element were determined.

Figure 3.6: X-ray photoelectron spectroscopy (XPS) from Ulvac Phi (model: Quanterra II).
3.3 Measurement of thermoelectric transport properties

3.3.1 Measurement setup for electrical resistivity ($\rho$) and the Seebeck coefficient ($\alpha$)

After the SPS process, one sample of each composition was cut into a bar shape as illustrated in Figures 3.7(a) and 3.7(b). Then, the Seebeck coefficient and electrical resistivity were measured simultaneously on the ZEM-3 (Ulvac-Riko) apparatus shown in Figure 3.7(c). The electrical conductivity was measured using a four-point probe method; therefore, the voltage decline could be neglected. The sample to be measured was held vertically in between two electrodes mounted on the upper and lower blocks. An electrical heater resistance was provided at the lower block, which was responsible for creating the temperature gradient along the sample length. Therefore, two pairs of chromel-alumel (type-K) thermocouples using two channels of a Keithley 2010 digital multimeter were used to measure temperatures $T_1$ and $T_2$ and the electric potential difference $dV$ between them across the sample. Using the electrodes, a small electric current $I$ runs through the sample, and the thermocouple wires measure the voltage difference $dE$ created by the current in the sample. These probes were spring loaded to ensure that there was good and direct contact between the probes and sample. Constant spacing was assumed between the two pairs of thermocouples and considered for the electrical resistivity and Seebeck coefficient calculations. From the $V$-$I$ curve, the resistance, and consequently the resistivity, can be determined at various temperatures. Voltage differences of the sample over different temperatures were used to calculate the Seebeck coefficient. Therefore, the Seebeck value was calculated from the slope of $\Delta V$ vs. $\Delta T$ plot. A schematic of the electrical resistivity and Seebeck coefficient measurements is given in Figure 3.8.

This arrangement was surrounded by a nickel radiation shield to ensure an isothermal environment. The setup was enclosed in an infrared furnace with a high purity helium atmosphere to prevent oxidation of the sample at elevated temperature measurements.
Sufficient pressure was applied in between the samples and all of the contact surfaces to reduce the contact resistance. To approximate the voltage losses over these contacts, which yield incorrect voltage values, the heat and current flow was in one dimension, and the distance between the probes and end plates was maintained 1.5 times larger than the samples’ characteristic lengths. The samples for the ZEM measurements were all rectangular in shape with an average size of 2 mmW×2 mm D×7 mm L ~ 4 mmW×4 mm D×9 mm L, and the measurement temperature range was from RT to 577 °C.

Figure 3.7: (a) Cutting the sample for electrical resistivity and Seebeck coefficient measurements, (b) final dimensions after cutting, and (c) the ZEM-3 (Ulvac-Riko) apparatus.
3.3.2 Measurement setup for thermal conductivity

The two surfaces of the sample prepared for the thermal conductivity measurement were parallel and flat. The first step was to attach thermocouples to the sample using a ceramic paste (see Figure 3.9(a)) for the temperature reading, followed by graphite coating as shown in Figure 3.9(b) to avoid a high laser reflection, which may reduce the energy absorption and induce a bad rear face signal. The thermal conductivity was measured with a TC-7000H (Ulvac-Riko) apparatus shown in Figure 3.9(c). A laser flash method was employed for the thermal conductivity measurement in the temperature range of RT-850 K. Liquid nitrogen was used for cooling below room temperature. The system included four main parts: the infrared furnace, the electronic control console, the detector assembly, and the sample holder. In the laser flash method, a laser pulse of 1 ms or less in width was used to momentarily heat the front side of a 10 mm diameter, 2 mm thick discoid sample, and the back side temperature change was measured. The temperature of the sample was detected by the thermocouples adjacent to the sample. The thermal conductivity was calculated using the relationship \( K = D \cdot C_p \cdot \rho_d \), with the thermal diffusivity \( D \) and specific heat \( C_p \) measured by a Flashline analyzer and a density of \( \rho_d \).
The lattice thermal conductivity $K_l$ was calculated by subtracting the electronic thermal conductivity $K_e$ from the measured $K$ using the Wiedemann-Franz law $K_e = L_0 T/\rho$
(assuming a temperature-independent Lorenz number $L_0 = 2.45 \times 10^{-8} \, V^2/K^2$).

![Figure 3.9](image)

**Figure 3.9:** (a) Preparation of the sample by fixing the thermocouple using a ceramic paste, (b) spraying of a thin layer of graphite to coat the sample, and (c) the TC-7000H (Ulvac-Riko) apparatus.

### 3.3.3 Measurement setup for the Hall mobility

The Lake Shore 8400 Series (see Figure 3.10) standard system used in this study is capable of DC field measurements and has a resistance range from 0.5 mΩ to 10 MΩ. It
measures the Hall voltage, Hall coefficient, Hall mobility, and resistivity. With added options, the system can measure down to 0.5 µΩ and as high as 200 GΩ in DC fields. The carrier density and carrier mobility versus temperature can also be determined in a temperature range of 10 K to 1273 K with a closed-cycle refrigerator and high-temperature oven. In this research, a single applied field was used to characterize the room temperature and temperature-dependent transport properties of the samples being studied, with sample dimensions of Φ = 10 mm and T = 1 mm, in a temperature range of RT to 227 °C.

![Image of the Lake Shore 8400 Series instrument](image)

**Figure 3.10:** The Lake Shore 8400 Series instrument for Hall mobility measurement.

### 3.4 Simultaneous Thermal Analysis (STA)

Figure 3.11 shows the simultaneous thermal analysis equipment from PerkinElmer (model: STA 6000) that was used in an operational range of RT to 1000 °C to
simultaneous measure and analyze the weight change and heat flow and thus indicate the thermal stability as well as the melting point temperatures. Combining differential scanning calorimetry (DSC) with proven thermogravimetry (TG) enabled the generation of accurate and reliable results while simplifying data interpretation. The measurements were performed from 25 °C to 1000 °C, heating up at a rate of 5 °C/min with 100 ml/min of N2 gas.

Figure 3.11: Simultaneous thermal analysis (STA) by a PerkinElmer instrument (model: STA 6000).

3.5 Measurement setup for mechanical properties (Vickers hardness)

The Vickers hardness was used to evaluate the ability of a thermoelectric element to resist plastic deformation from a standard source. The Shimadzu G21 series micro-hardness tester shown in Figure 3.12 was employed for this measurement under a load of 1 N sustained for 10 seconds. The micro-hardness was computed by the following equation:
\[ HV = 1.891 \frac{F}{d^2} \]

where HV is the Vickers hardness in MPa, F is the force in Newtons, and d is the average length of the diagonals of the indent in mm.

*Figure 3.12: A Shimadzu G21 series micro hardness tester*
CHAPTER 4: RESULTS AND DISCUSSION

In this chapter, the analysis of Mn, Hf, and Al in a CoSb$_3$ binary skutterudite material and of Al and Bi in a Yb$_{0.25}$Co$_4$Sb$_{12}$ ternary skutterudite thermoelectric material will be discussed. The formulations will be discussed individually in the context of microstructural, thermoelectric, electronic, thermal and hardness properties. In the first 3 formulations, the effect of doping (Mn, Hf, and Al) on the binary CoSb$_3$ will be discussed. In this section, a spin crossover behavior from n-p type for the formulation Al$_{0.3}$Co$_4$Sb$_{12}$ will also be presented. Next, the effect of excess doping on the microstructural and thermoelectric behaviors using Al as a case study will be elaborated. Finally, extension of doping to the ternary skutterudite Yb$_{0.25}$Co$_4$Sb$_{12}$ formulation using Al and Bi will be discussed to demonstrate the achievement of a high $ZT$ using strategies to manipulate the grain boundary morphology.

4.1 Mn-added CoSb$_3$ composition

Manganese has been widely used as a main element in half and full Heusler alloy thermoelectric materials (Dyck et al., 2002; Hornbostel et al., 1997; Nolas et al., 2005; Park et al., 2014) as well as in higher manganese silicide thermoelectric materials (Luo et al., 2011; Ponnambalam et al., 2013; Saleemi et al., 2015; A. J. Zhou et al., 2010; A. Zhou et al., 2012).

In this section, Mn which has a small atomic radius, is proposed as an alternative loosely bonded filler element for the CoSb$_3$ skutterudite thermoelectric material. This approach is in contrast to the substitution approach tackled by previous research involving transition metals. For example, Mn has been used to substitute the Co side in CoSb$_3$ skutterudite (Park et al., 2014). (Kitagawa et al., 2005) prepared a single phase of skutterudite by doping Ni into the CoSb$_3$ matrix, and they found that the lattice parameter increased linearly with an increasing Ni content, indicating that the Ni atoms occupy the
Co site in the skutterudite structure. This finding was extended to include an Fe-doped CoSb$_3$ matrix in the study conducted by (Ur et al., 2007), whose found that Fe could also occupy the Co site without forming a secondary phases. Thus, it will be interesting to observe whether the doping of Mn in to the CoSb$_3$ system will succeed in filling the skutterudite voids.

4.1.1 Microstructural properties

The MAed powders were strongly deformed by the high impact of mechanical energy, and they were thermodynamically metastable (Yang et al., 2006). During the SPS process the elements were almost completely reacted into the skutterudite phase; therefore, a polycrystalline phase of filled skutterudite with a secondary phase of MnO were obtained and presented in the as-sintered XRD pattern shown in Figure 4.1. The cubic-type skutterudite structure (Im-3 space group) with a room temperature lattice constant of $a = 9.0340$ Å was obtained in this study, which is lower than the value of $9.0345$ Å for the single crystalline CoSb$_3$. Furthermore, a small shift in the position of the binary skutterudite CoSb$_3$ (Kawaharada et al., 2001) was observed for the Mn-added CoSb$_3$. The change in the valence state and structure defect due to strain as a result of Mn substitution might be the reasons for contraction in the lattice constant as well as the shift in the 2 theta value. Furthermore, the effect of the small radii of Mn compared to the radii of Co may result in a decreased lattice parameter of CoSb$_3$, while the elements with an identical or larger radii as Co (i.e., Fe, Ni and In) (Kitagawa et al., 2005; Mallik et al., 2008; Peng et al., 2004) may result in an increased lattice parameter.
Figure 4.1: XRD pattern of the as-sintered sample of Mn-added Co$_4$Sb$_{12}$

The actual density for the as-sintered sample was found to be 6.7 g/cm$^3$. This relatively high density is in agreement with the small number of pores observed in the SEM micrograph image shown in Figure 4.2(a). The average grain size was less than 5 µm. The composition of the grains and the grain boundaries were investigated by EDX (Table 4.1) and are explained in Figure 4.2(a). This indicates that Mn atoms substituted the Co sites inside the grains rather than filling the skutterudite voids. However, an excess amount of Mn atoms was indicated in the grain boundaries, as well as substitution of Co sites by Mn atoms. Furthermore, the elemental mapping shown in Figure 4.2(c) indicates that Mn takes on various microstructural modification roles within the skutterudite; Mn distributed systematically in the grains, agglomerated as Mn-rich regions at the edges of the grains, and formed a nano-sized Mn-containing secondary phase along the grain boundaries. This behavior agrees with the Bi-filling CoSb$_3$ described in the work of
Mallik et al. (2013), although Bi is a heavy atom element. However, most of the lanthanides and alkali earth metals tended to fill the voids of the CoSb$_3$ without making secondary phases, if a suitable fraction was used. We can also observe some Co-rich regions in Figure 4.2(d) that might have been formed as a result of the substitution of Mn instead of Co in the skutterudite phase.

Table 4.1: EDX results indicating the actual composition of Mn-added CoSb$_3$

<table>
<thead>
<tr>
<th>Position</th>
<th>No.</th>
<th>Element</th>
<th>Grain composition (Atomic %)</th>
<th>Grain boundary compositions (Atomic %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Mn</td>
<td></td>
<td>2.18</td>
<td>8.70</td>
</tr>
<tr>
<td>2</td>
<td>Co</td>
<td></td>
<td>23.33</td>
<td>20.82</td>
</tr>
<tr>
<td>3</td>
<td>Sb</td>
<td></td>
<td>74.49</td>
<td>70.48</td>
</tr>
</tbody>
</table>
Figure 4.2: SEM images of MnCo$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, and (b) an SEM/EDX micrograph. The elemental mapping of (c), (d), and (e) show Mn, Co, and Sb, respectively, extracted from (b) using EDX.
4.1.2 Thermoelectric properties

The electrical resistivity for the Mn-added CoSb$_3$, at the measured temperature region (RT – 577 °C) shown in Figure 4.3(a) indicates a slight decrease in the electrical resistivity of the binary skutterudite CoSb$_3$ (Kawaharada et al., 2001). The high resistivity of the skutterudite modified by Mn-addition compared to the lanthanides and alkali earth metals additions can be attributed to the presence of the MnO secondary phase which provides additional interfaces in the bulk of the material. The increased number of interfaces in the samples may lead to additional scattering of the carriers, which could result in high resistivity (Mallik et al., 2013). Moreover, due to the increase in the carrier concentration and excitation of the carriers across the band gap, the electrical resistivity decreased with increasing temperature, exhibiting a semiconducting behavior (Laufek et al., 2009).

Figure 4.3(b) shows the temperature dependence of the Seebeck coefficient ($\alpha$) for the Mn-added CoSb$_3$. A positive Seebeck coefficient was observed, indicating a p-type thermoelectric material. A tiny increase in the value of $\alpha$ was realized from RT until 127 °C, at which point there was a peak with a value of 242 μVK$^{-1}$; there was then a dramatic decrease from 127 °C to 577 °C when the intrinsic effect of manganese becomes active. The absolute value of the Seebeck coefficient of Mn-added CoSb$_3$ is larger than that of CoSb$_3$ (~225 μVK$^{-1}$) (Kawaharada et al., 2001). The power factor (PF) exhibits a parabola-like behavior (see Figure 4.3(c)) due to the reverse interrelationship between the Seebeck coefficient and the electrical conductivity. A maximum PF of $0.39 \times 10^{-3}$ Wm$^{-1}$K$^{-2}$ was obtained at 277 °C.
Figure 4.3: Temperature dependence of the (a) electrical resistivity, (b) Seebeck coefficient, and (c) power factor ($PF$).
Figure 4.4(a) shows the temperature dependence of the thermal conductivity ($K$). The thermal conductivity decreased with an increase in temperature up to 500 K, at which point $K = 3.3 \text{ W/m.K}$ (the minimum thermal conductivity of the CoSb$_3$ binary skutterudite is $\sim 4.5 \text{ W/m.K}$ (Kawaharada et al., 2001)). Generally, the scattering of lattice vibrations becomes more vigorous with the rise of temperature. However, the thermal conductivity increased gradually from 500 K to 850 K, indicating less phonon scattering from the interfacial phase of MnO located in the grain boundaries. The lattice thermal conductivity, $K_L$, can be estimated by subtracting the electronic contribution, $K_e = LT/\rho$, from the total thermal conductivity, where $L = 2.45 \times 10^{-8} \text{ V}^2\text{K}^2$ is the Lorenz number. As shown in Figure 4.4(b), $K_L$ was highly suppressed compared with the lattice thermal conductivity of CoSb$_3$ reported in the work of Zhang et al. (2015) due to the addition of Mn, which created a highly disordered lattice structure that was more effective in phonon scattering. Thus, the relative contribution of electron thermal conductivity to the total thermal conductivity was negligible. It is therefore evident that small and light Mn atoms are effective in reducing heat-carrying phonons. Consequently, Mn is a promising candidate for multiple doping in CoSb$_3$ materials with a heavy atom element. However, a low $ZT$ of 0.06 at 577 K, as shown in Figure 4.4(c), was found as a result of high electrical resistivity, although the thermal conductivity was reduced.
Figure 4.4: Temperature dependence of the (a) thermal conductivity, (b) lattice thermal conductivity, and (c) Figure of merit $ZT$. 
4.1.3 Thermal behavior

Figure 4.5 indicates the thermal stability of the Mn-added CoSb$_3$ composition. The TGA thermograph in Figure 4.5(a) shows a great stability of the skutterudite phase up to 644 °C, at which point weight reduction begins to occur as a result of Sb sublimation. The total decomposition of the skutterudite phase was observed at 854 °C. The new resultant phases began to decompose at 921 °C. In Figure 4.5(b), the DSC thermograph contains only one endothermic peak, from which the onset melting point of the skutterudite phase was determined to be over 850 °C. The melting points of the residuals phases were indicated through the sub-endothermic peaks at 887 °C and 962 °C.

Figure 4.5: (a) TGA, and (b) DSC; thermographs upon heating of the Mn-added Co$_4$Sb$_{12}$ composition.
4.1.4 Mechanical properties

To assess the homogeneity of the Mn-added CoSb₃ sample, micro-hardness was mapped on several cross-sections of the specimen. A homogeneous distribution of HV₀.₁ values in the range of 622-632 was observed with no significant differences between the different regions of the sample’s margins and interior area, thus emphasizing the suitability of the SPS process for producing dense samples with a uniform microstructure. Moreover, the addition of Mn to CoSb₃ increased the HV value of the binary skutterudite CoSb₃, which was reported by Recknagel et al. (2007) to be 608.

4.2 Hf-added CoSb₃ composition

Ongoing work to explore new filling species and evaluate their contribution to thermoelectric properties is greatly needed to fill in the knowledge gap for this type of thermoelectric material. Replacing the lanthanum cation by a cation with a smaller ionic radius and higher mass has been predicted to result in skutterudites with a thermal conductivity less than any thermal conductivity of a known thermoelectric material (Hornbostel et al., 1997; Nolas et al., 2005). Therefore, hafnium as a heavy atom element can work as an alternative loosely bonded filler element for the CoSb₃ skutterudite thermoelectric material. In this section, filling the voids of CoSb₃ skutterudite with Hf will be investigated. However, although the heavy atom elements tend to fill the voids of CoSb₃ without making secondary phases, some secondary phase formations are possible as a result of the fabrication process, for example. Yb₂O₃ and YbSb phases were formed in the skutterudite matrix of Yb₀.₂In₀.₂Co₄Sb₁₂ in the work of Ballikaya et al. (2012).

4.2.1 Microstructural properties

The MAed powders were strongly deformed and thermodynamically metastable as a result of the high impact of mechanical energy (Yang et al., 2006). After the SPS process,
a polycrystalline phase of filled-skutterudite with a small peak for HfO$_2$ as a secondary phase were obtained and are presented in the as-sintered XRD pattern shown in Figure 4.6. The crystal structure was refined using JANA2006. The lattice parameter was refined to be $a = 9.03454(8)$ ångstrom and the occupancy of Hf at 12d site was refined to be $0.0429(11)$, yielding the composition of Hf$_{0.514(13)}$Co$_8$Sb$_{24}$ (Hf$_{0.257}$Co$_4$Sb$_{12}$). The mass ratio of skutterudite and HfO$_2$ is refined to be 93.9(6) % and 6.1(4) %, respectively, as the strongest peak of HfO$_2$ is only observed at 2 theta = 28.2, as a broad peak.

![XRD pattern of the as-sintered sample of Hf-added Co$_4$Sb$_{12}$](image)

**Figure 4.6:** XRD pattern of the as-sintered sample of Hf-added Co$_4$Sb$_{12}$.

The actual density for the as-sintered sample was more than 99% of the calculated density. This relatively high density agrees with the small number of pores observed in the SEM micrograph image shown in Figure 4.7(a). The grains size was variable. The average size was 7 µm for the majority of the grains, and the presence of a few large grains with sizes up to 45 µm were observed. The composition of the grains and the grain boundaries were investigated by EDX. The atomic percent indicated that the Hf atoms
might partially fill the skutterudite voids inside the grains, whereas an excess amount of Hf atoms was detected in the grain boundaries. Furthermore, the elemental mapping shown in Figures 4.7(c,d,e) indicates that Hf takes on two microstructural modification roles within the skutterudite. Specifically, Hf distributes equally in the whole region of the grains and also agglomerates as Hf-rich regions at the edges of the grains or along the grain boundaries. This behavior agrees with that of the Pr-filling CoSb₃ discussed in the work of (Graff et al. 2014) and of the Bi-filling CoSb₃ discussed in the work by Mallik et al. (2013). However, the tendency of Hf to fill the voids of CoSb₃ has been confirmed in this study, although an excess amount of Hf was found to agglomerate in the grain boundaries. Therefore, a single phase of Hf-filled skutterudite could be obtained if the suitable fraction was used.
Figure 4.7: The SEM images of Hf-filled CoSb$_3$; (a) a micrograph of an SPS-compacted sample, and (b) a SEM/EDX micrograph; the elemental mapping of (c), (d), and (e) show Hf, Co, and Sb, respectively, extracted from (b) using EDX.
4.2.2 Thermoelectric properties

The electrical resistivity of the Hf-filled CoSb$_3$, at the measured temperature region (RT – 577 °C) shown in Figure 4.8(a) indicated a slight reduction from the electrical resistivity of the binary skutterudite CoSb$_3$ (Kawaharada et al., 2001). Essentially, due to its electronic structure in the composition, HfO$_2$ has less of an impact on the carrier concentration; therefore, the electrical resistivity remained high. The electrical resistivity decreased with increasing temperature, displaying a semiconducting behavior, which is a result of increasing the carrier concentration and excitation of the carriers across the band gap (Laufek et al., 2009).

Figure 4.8(b) shows the temperature dependence of the Seebeck coefficient ($\alpha$) for the Hf-filled CoSb$_3$. A positive Seebeck coefficient was observed, indicating a p-type thermoelectric material. A tiny increase in value of $\alpha$ can be realized from RT to 150 °C, at which point there is a peak with a value of 153 $\mu$VK$^{-1}$; there is then a dramatic decrease from 150 °C to 550 °C, when the intrinsic effect of hafnium becomes active. The absolute value of the Seebeck coefficient of Hf-filled CoSb$_3$ is less than that of CoSb$_3$ (~225 $\mu$VK$^{-1}$) (Kawaharada et al., 2001). The power factor ($PF$) exhibits a parabola-like behavior (see Figure 4.8(c)) due to the reverse interrelationship between the Seebeck coefficient and the electrical conductivity. A maximum $PF$ of $0.143 \times 10^{-3}$ Wm$^{-1}$K$^{-2}$ was obtained at 300 °C.
Figure 4.8: Temperature dependence of the (a) electrical resistivity, (b) Seebeck coefficient, and (c) power factor (PF).
Figure 4.9(a) shows the temperature dependence of the thermal conductivity ($K$). As illustrated, the thermal conductivity decreased with an increase in temperature up to 500 K, at which point $K = 1.8 \text{ W/m.K}$ (the minimum thermal conductivity of the CoSb$_3$ binary skutterudite is $\sim 4.5 \text{ W/mK}$ (Kawaharada et al., 2001)). For the most part, the phonon scattering tended to be forceful with the rise in temperature. However, the thermal conductivity increased gradually from 500 K to 850 K, indicating less phonon scattering from the rattling modes of the filling atoms.

The lattice thermal conductivity, $K_L$, can be estimated by subtracting the electronic contribution, $K_e = LT/\rho$, from the total thermal conductivity, where $L = 2.45 \times 10^{-8} \text{ V}^2\text{K}^2$ is the Lorenz number (Park & Kim, 2010). As shown in Figure 4.9(b), $K_L$ is extremely suppressed compared with the lattice thermal conductivity of CoSb$_3$ reported by Zhang et al. (2015). The dramatic reduction of the thermal conductivity in the Hf-added skutterudite sample mainly comes from the oscillation of the loose bond. Principally, due to the anharmonicity of the oscillation of the guest atom, the phonon scattering could be increased. Likewise, the point defects on the lattice microstructure caused by nano-scale aggregations of Hf atoms and the large area fraction of the grain boundaries might be the reasons for the significant drop in the thermal conductivity of Hf-filled CoSb$_3$. Therefore, the disorder in the lattice structure caused by the addition of Hf was the reason for the increase in phonon scattering, hence decreasing the lattice thermal conductivity.

Furthermore, the relative contribution of the electron thermal conductivity to the total thermal conductivity was negligible. It is therefore perceptible that Hf atoms are effective in reducing heat-carrying phonons. Consequently, Hf is a promising candidate for the multi-filling of CoSb$_3$ skutterudite, if used with one or more rare earth elements. However, a low $ZT$ of 0.04 at 577 K, as shown in Figure 4.9(c), was found as a result of the high electrical resistivity, although the thermal conductivity was significantly reduced.
Figure 4.9: Temperature dependence of the (a) thermal conductivity, (b) lattice thermal conductivity, and (c) Figure of merit $ZT$. 
4.2.3 Thermal behavior

Figure 4.10 shows the thermal stability of the Hf-added CoSb$_3$ composition. The TGA thermograph in Figure 4.10(a) shows the great stability of the skutterudite phase up to 645 °C, at which point weight reduction begins to occur as a result of Sb sublimation. The total decomposition of the skutterudite phase was observed at 866 °C. The new resultant phases began to decompose at 945 °C. From Figure 4.10(b), the DSC thermograph shows only one endothermic peak, from which the onset melting point of the skutterudite phase was determined to be over 800 °C. The melting point of the residual phase was indicated through the sub-endothermic peak at 910 °C.

![TGA thermograph](image)

![DSC thermograph](image)

**Figure 4.10:** (a) TGA, and (b) DSC; thermographs upon heating of the Hf-added Co$_4$Sb$_{12}$ composition.
4.2.4 Mechanical properties

To assess the homogeneity of the Hf-added CoSb$_3$ sample, micro-hardness was mapped on several cross-sections of the specimen. A homogeneous distribution of HV$_{0.1}$ values in the range of 362-366 was observed, with no significant differences between the different regions of the sample’s margins and interior area, thus emphasizing the suitability of the SPS process for producing dense samples with a uniform microstructure. However, the addition of Hf to CoSb$_3$ significantly decreased the HV value of the binary skutterudite CoSb$_3$, which was reported by Recknagel et al. (2007) to be 608. This may be attributed to the increase in the area fraction of the grain boundaries from the addition of Hf.

4.3 Al$_x$-added CoSb$_3$ compositions (x = 0.3, 0.6, 2)

From the previous sections, transition elements were found to be very effective in reducing the thermal conductivity. Thus, in this work, the search for elements other than the alkaline earth metal and lanthanide elements to reduce the thermal conductivity of CoSb$_3$ skutterudite was extended to cover other metal elements such as Al. In this section, an excess amount of Al-doping was used to modify the grain boundary of the formulation. The accumulation of Al in the grain boundaries will serve to reduce the thermal conductivity of CoSb$_3$ skutterudite without affecting the electrical conductivity or Seebeck coefficient. Therefore, it is interesting to discuss the influence of dopants other than the alkaline earth metal and lanthanide elements on the structure of CoSb$_3$ skutterudite for a complete understanding of the crystal formation of this type of composition.

However, there are many factors affecting the formations of the ternary skutterudite matrix, such as the fabrication process, the stoichiometry of the elements in the
composition, and the ionic radius and atomic mass of the dopant. For example, the Te-doped CoSb$_3$ matrix in the work of Wojciechowski (2002) resulted in a Te-containing secondary phase. Later, Kim and Kim (2010) were able to obtain a single phase of skutterudite for Te-doped CoSb$_3$ with a slight modification of the fabrication process. Sn has been determined to fill the lattice voids of CoSb$_3$ and form a single phase of skutterudite in the work of Mallik et al. (2007), while, in a previous study by Kim et al. (2007) from same year, Sn was shown to occupy the Sb site and form a single phase of skutterudite that contained Sn in the mixture up to CoSb$_{2.6}$Sn$_{0.4}$; otherwise, Sn-containing secondary phases have been detected. Indium has shown promise as a skutterudite filler, which can form a single phase (Mallik et al., 2008) or in some cases a secondary phase of InSb (G. Li et al., 2012).

4.3.1 Microstructural properties

The XRD for as-sintered samples shown in Figure 4.11 indicates that the influence of the spark plasma sintering process on the metastable MA powders was very efficient. As a result, the MA powders were highly compacted to a polycrystalline skutterudite phase with different amounts of an AlSb secondary phase. The presence of AlSb was found to vary according to the amount of Al added to the Co$_4$Sb$_{12}$ (CoSb$_3$) binary skutterudite system. The sharp peak of AlSb that appeared in the Al$_2$Co$_4$Sb$_{12}$ sample decreased with the decrease in aluminum addition. The lattice parameters fluctuated with the change in the amount of the Al addition in the structure of Al$_x$Co$_4$Sb$_{12}$ (x = 0.3, 0.6, 2), which were reported as 9.0385 Å, 9.0375 Å and 9.0394 Å, respectively. However, two alternative models can be predicted for Al-doped binary skutterudite: A: Al substituted for Sb in the 24g (0, y, z) site or B: Al filled the voids in the 2a (0, 0, 0) site.
Figure 4.11: XRD patterns of the as-sintered sample of Al<sub>x</sub>Co<sub>4</sub>Sb<sub>12</sub> (x = 0.3, 0.6, 2)

The SEM micrographs of the as-sintered samples of Al<sub>x</sub>Co<sub>4</sub>Sb<sub>12</sub> (x = 0.3, 0.6, 2) shown in Figure 4.12(a), Figure 4.13(a) and Figure 4.14(a), respectively, indicated very interesting surface topographies. The topographical feature of the Al<sub>0.3</sub>Co<sub>4</sub>Sb<sub>12</sub> sample was the formation of small grains with non-uniform grain boundaries. This feature was altered in the Al<sub>0.6</sub>Co<sub>4</sub>Sb<sub>12</sub> sample, which contained large grains surrounded by well-defined grain boundaries. In the Al<sub>2</sub>Co<sub>4</sub>Sb<sub>12</sub> sample, a combination of large and small grains was indicated. The shrinkage in the size of some grains can be attributed to the large grain boundaries that formed as a result of an excess amount of added Al. Generally, the size of the grain boundaries was proportional to the amount of Al added.

We verified the presence of the AlSb phase in the grain boundaries of all samples using SEM/EDX, and further investigation was performed on the Al<sub>0.3</sub>Co<sub>4</sub>Sb<sub>12</sub> sample using FIB/TEM. Moreover, elemental mapping was utilized to further investigate the microstructure and actual composition of the samples. The elemental mapping of the as-
sintered samples of Al\textsubscript{x}Co\textsubscript{4}Sb\textsubscript{12} (x = 0.3, 0.6, 2) shown in Figures 4.12(c, d, e), Figures 4.13(c, d, e), and Figures 4.14(c, d, e), respectively, clearly illustrates the distribution of the ternary system elements. The Co and Sb elements were distributed in a systematic order in the surface of the grains of the as-sintered samples, whereas the existence of Al inside the grains was shown to be less than 2 wt%. A strong presence of Al next to Sb in the grain boundaries was obtained. The presence of Al beside Sb in the grain boundaries agrees with the AlSb peak indicated in the XRD graph. The Al atoms appeared as rich spots in the grain boundaries of Al\textsubscript{0.3}Co\textsubscript{4}Sb\textsubscript{12} in Figure 4.12(c), which increased with the increasing amount of Al doping in Al\textsubscript{0.6}Co\textsubscript{4}Sb\textsubscript{12} in Figure 4.13(c). The clustering of the Al dopant at the edge of the grains and in the grain boundaries of the Al\textsubscript{2}Co\textsubscript{4}Sb\textsubscript{12} sample became very solid and almost fully enclosed the skutterudite grains (see Figure 4.14(c)).

If we look closer at the microstructure of the Al-doped CoSb\textsubscript{3} in Figure 4.15(a), we can realize that the grain boundaries contain of two types of small grains. The majority of these grains are shown to be skutterudite, as investigated by TEM/EDX, and these skutterudite grains have some small AlSb grains in between them, which gives an overview of the growth of AlSb in the grain boundaries. By increasing the Al doping, the small skutterudite grains in the grain boundaries could be replaced by AlSb grains. Figure 4.15(b) shows that different types of skutterudite small grains could be obtained in the grain boundary areas, such as fully crystallite grains (region A), polycrystalline grains (region B) and almost amorphous grains (region C). This can be attributed to the Al contained in the grain microstructure. As the amount of Al in the grain increased, the disorder of the lattice structure became higher. To determine the elemental distribution, EDX and elemental mapping were performed to extract the Al, Co and Sb from the area illustrated in the box frame of the image shown in Figure 4.15(c). The EDX result in Figure 4.15(d) showed an excess amount of Al with a satisfactory percentage of CoSb. The Cu indicated in the sample came from the cupper grid finger attached to the lamella.
The mapping of the elements shown in Figures 4.15(e, f, g) confirmed the presence of the AlSb phase, as expected. However, in recent studies, InSb clusters have appeared as a secondary phase in In-doped CoSb$_3$, rather than entering the Sb icosahedral voids, with demonstrated improvements in electrical performance and consequently TE efficiencies (Graff et al., 2011; Li et al., 2009; Peng et al., 2009). Therefore, we can conclude that Al doping is very effective in the lattice disorder of the skutterudite matrix and can be used to improve the thermoelectric properties of the skutterudite system, as well as other open structure systems.
Figure 4.12: SEM images of Al$_{0.3}$Co$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, and (b) an SEM/EDX micrograph; the elemental mapping of (c), (d), and (e) show Al, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.13: SEM images of Al$_{0.6}$Co$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, and (b) an SEM/EDX micrograph; the elemental mapping of (c), (d), and (e) show Al, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.14: SEM images of Al$_2$Co$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, and (b) an SEM/EDX micrograph; the elemental mapping of (c), (d), and (e) show Al, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.15: TEM images of Al$_{0.3}$Co$_4$Sb$_{12}$; (a) micrograph of an SPS-compacted sample at a magnification of 26.5KX; (b) micrograph of an SPS-compacted sample at a magnification of 530KX showing fully crystallite grains (region A), polycrystalline grains (region B) and almost amorphous grain (region C); (c) a TEM/EDX micrograph; (d) integrated EDX spectrum extracted from the box frame area in (c); the elemental mapping of (e), (f), and (g) show Sb, Co, and Al, respectively, extracted from the box frame area in (c) using the EDX.
4.3.2 Thermoelectric properties

The temperature dependence of electrical resistivity for the Al$_x$Co$_4$Sb$_{12}$ ($x = 0.3, 0.6, 2$) samples shown in Figure 4.16(a) demonstrated high electrical resistivity at room temperature for all compositions in comparison with the skutterudite system filled with heavy atoms, such as Yb (Li et al., 2009). The electrical resistivity of the compositions decreased with increasing temperature, indicating a semiconductor behavior over the entire temperature range for all samples. The most stable sample with the narrowest electrical resistivity range was the one with the highest amount of AlSb nano-inclusions in its composition, which was Al$_2$Co$_4$Sb$_{12}$. However, the high amount of impurities and defects that can be produced by nano-inclusions in the crystal lattice of the skutterudite matrix may cause new additional electronic states within the bandgap and act to trap the charge carriers. Therefore, most previous research has shown an increase in the average electrical resistivity as a result of introducing nano-inclusions in skutterudite compositions. Thus, this finding is novel in that it demonstrates a reversed and desirable behavior.

Figure 4.16(b) shows the temperature dependence of the Seebeck coefficient for Al$_x$Co$_4$Sb$_{12}$ ($x = 0.3, 0.6, 2$). Almost, similar pattern of temperature dependence of the Seebeck coefficient was recorded for the Al$_{0.6}$Co$_4$Sb$_{12}$ and Al$_2$Co$_4$Sb$_{12}$ samples. The highest Seebeck coefficient recorded for both of these samples was 218 µV/K and 198 µV/K at 127 °C, respectively. The positive sign that appeared in the Seebeck coefficient values for these two samples indicates p-type behavior. Unusual behavior of the temperature dependence of the Seebeck coefficient was observed for the Al$_{0.3}$Co$_4$Sb$_{12}$ sample. Thus, Seebeck coefficient crossover (n- to p-type) at a reverse point of 200 °C was recorded. The tiny deviation of the cooling curve from the heating curve at lower temperatures can be attributed to the relaxation time. Similar behavior was obtained by Kawaharada et al. (2001) for the ternary skutterudite CoSb$_3$ with added Bi. The nature of
p-type or n-type in misleading CoSb$_3$ can be attributed to the chemical purity of the starting material, as contaminations may introduce dopants. A slight lack of Sb leads to n-type conductivity, while a lack of Co leads to p-type conductivity. The transition from negative to positive values of the Seebeck coefficient is usually observed in the CoSb$_3$ samples that are uncompensated at the Sb site. In general, a transition occurs when the carrier type changes from being weakly extrinsic to intrinsic due to an increased temperature (Mallik et al., 2013).

However, regarding the Al$_{0.3}$Co$_4$Sb$_{12}$ composition, Table 4.2 shows that the electron concentration ($n$), as well as the hall mobility ($\mu_H$), decreased with increasing temperature up to 127 °C, and the contribution of holes increased as the sign changed from negative to positive at 177 °C. Therefore, the sample exhibited p-type behavior after 200 °C as a result of the increasing hole concentration with the increase in temperature. In Figure 4.6(b), the Seebeck curves were almost identical upon heating and cooling. Thus, this behavior can be attributed to the change in the spin status of Co(III) from low spin (LS) to high spin (HS). XPS was used to determine the chemical state of Co, and, at room temperature, the composition contained 64% Co(II) and 36% Co(III). In situ HT-XRD was used to determine the change in the bond length of Co-Sb as a function of temperature, and the bond length of Co-Sb increased from 2.519 Å at room temperature to 2.523 Å at 200 °C. Thus, in this SCO composition, an external heat source is proposed to drive the following transition:

\[
\text{RT} - 200 ^\circ C \xrightarrow{\text{Heating}} \text{HS Co(II)} + \text{LS Co(III)} \xrightarrow{\text{Cooling}} 200 - 527 ^\circ C \xrightarrow{\text{Heating}} \text{HS Co(II)} + \text{HS Co(III)}
\]

Moderate power factors were reported for Al$_x$Co$_4$Sb$_{12}$ ($x = 0.3, 0.6, 2$), as shown in Figure 4.16(c). The highest power factor of $0.41 \times 10^{-3}$ W/m.K$^2$ belonged to the Al$_{0.3}$Co$_4$Sb$_{12}$ sample at 377 °C. A small reduction of this value was realized at $0.40 \times 10^{-3}$
W/m.K² for the Al₀.₆Co₄Sb₁₂ sample at a lower temperature of 327 °C. With the increase in the amount of Al added to the Al₂Co₄Sb₁₂ sample, the maximum power factor value decreased to 0.34×10⁻³ W/m.K² at a medium temperature of 277 °C.

Table 4.2: Temperature dependent transport properties of AlₓCo₄Sb₁₂ (x = 0.3, 0.6, 2).
Figure 4.16: Temperature dependence of the (a) electrical resistivity, (b) Seebeck coefficient, and (c) power factor (PF) for Al$_x$Co$_4$Sb$_{12}$ ($x = 0.3, 0.6, 2$) compositions.
In Figure 4.17(a) the temperature dependence of the thermal conductivity ($K$) was demonstrated for $\text{Al}_x\text{Co}_4\text{Sb}_{12}$ ($x = 0.3, 0.6, 2$). The minimum thermal conductivity ($K_{\text{min}}$) for all samples was recorded at elevated temperatures. The $K_{\text{min}}$ for the $\text{Al}_{0.3}\text{Co}_4\text{Sb}_{12}$ sample was found to be 4.6 W/m.K at 600 K, whereas this value decreased significantly for the $\text{Al}_{0.6}\text{Co}_4\text{Sb}_{12}$ sample to 3.3 W/m.K at 500 K. The most significant reduction in $K$ of 2.7 W/m.K was obtained for the sample with a high Al content, which was $\text{Al}_2\text{Co}_4\text{Sb}_{12}$. The lattice thermal conductivity, $K_L$, can be estimated by subtracting the electronic contribution of the Wiedemann-Franz law, $K_e = LT/\rho$, from the total thermal conductivity, where $L = 2.45 \times 10^{-8} \text{ V}^2\text{K}^2$ is the Lorenz number (Park & Kim, 2010). As shown in Figure 4.17(b), $K_L$ was suppressed by a tiny amount for all samples compared with the $K_L$ of the skutterudite $\text{CoSb}_3$ filled with heavy elements. Therefore, the minimum $K_L$ values were 4.4 W/m.K, 3.2 W/m.K and 2.6 W/m.K at 600 K, 500 K and 500 K for $\text{Al}_x$ ($x = 0.3, 0.6, 2$), respectively. The electronic contribution $K_e$ had a negligible effect on the total thermal conductivity in this system. However, the addition of Al to the binary skutterudite $\text{CoSb}_3$ resulted in a decrease in the thermal conductivity of ~45% for the $\text{Al}_2\text{Co}_4\text{Sb}_{12}$ composition compared with the binary skutterudite $\text{CoSb}_3$ discussed in the work of Kawaharada et al. (2001).

Composites of $\text{Al}_x\text{Co}_4\text{Sb}_{12}/\text{AlSb}$ demonstrated a high electrical resistivity, a high Seebeck coefficient and a relatively low lattice thermal conductivity. Therefore, the high electrical resistivity contributed to low figures of merit $ZT$s of 0.047, 0.066 and 0.061 at one operating temperature of 600 K (see Figure 4c) for $\text{Al}_x\text{Co}_4\text{Sb}_{12}$ ($x = 0.3, 0.6, 2$), respectively.
Figure 4.17: Temperature dependence of the (a) thermal conductivity, (b) lattice thermal conductivity, and (c) Figure of merit $ZT$ for $\text{Al}_x\text{Co}_4\text{Sb}_{12}$ ($x = 0.3, 0.6, 2$) compositions.
4.3.3 Thermal behavior

Figures 4.18 and 4.19 show the thermal stability of Al\textsubscript{x}-added CoSb\textsubscript{3} compositions (x = 0.3, 0.6, 2). The TGA thermograph in Figure 4.18(a) shows the great stability of the x = 0.3 composition up to 400 °C, at which point weight gain began up to 534 °C as a result of oxidation. Then, a rapid weight loss can be observed from 534°C to 600 °C, attributed to the sublimation of impurities in the starting materials and/or the evaporation of moisture gained during sample preparation for STA. The sublimation of Sb began to occur from 644 °C and was associated with weight reduction until 827 °C, at which point the decomposition of the skutterudite phase was observed. The new resultant phases began to decompose immediately at 854 °C. From Figure 4.18(b), no oxidation behavior was observed up to 520 °C for the x = 0.6 composition. From 520 °C to 564 °C, a small decrease in weight can be observed, attributed to the sublimation of impurities in the starting materials and/or the evaporation of the moisture gained during sample preparation for STA. At 634 °C, the sublimation of Sb began to occur and was associated with weight reduction until 839 °C, at which point the decomposition of the skutterudite phase was observed. In the x = 2 composition shown in Figure 4.18(c), great thermal stability was realized up to 647 °C, at which point the sublimation of Sb began to occur, leading to gradual weight loss up to 847 °C. Above 847 °C, rapid weight loss was indicated and attributed to decomposition of the skutterudite phase. It can be concluded that the thermal stability increased significantly with increasing amounts of added Al.

In Figure 4.19, the DSC thermograph shows one endothermic peak, which indicates the melting points for the x = 0.3, 0.6 and 2 compositions. The onset melting point of x = 0.3 and 0.6 was observed to be over 800 °C (see Figures 4.19(a) and 4.19(b)), which can be attributed to the skutterudite phase. However, in the x = 2 composition (see Figure 4.19(c)), there is no indication of a clear onset melting point of the skutterudite phase, although a small endothermic peak was observed at 911 °C for the AlSb phase.
Figure 4.18: TGA thermographs upon heating of Al$_x$-added Co$_4$Sb$_{12}$ compositions: (a) $x = 0.3$, (b) $x = 0.6$, and (c) $x = 2$. 
4.3.4 Mechanical properties

To assess the homogeneity of the Al$_x$-added Co$_4$Sb$_{12}$ samples ($x = 0.3, 0.6, 2$), micro-hardness was mapped on several cross-sections of the specimens. A homogeneous distribution of HV$_{0.1}$ with average values of 499, 469, and 436 was observed for the Al$_x$-
added CoSb₃ compositions (x = 0.3, 0.6, 2), respectively. There were no significant differences between the different regions of the samples’ margins and interior areas, thus emphasizing the suitability of the SPS process for producing dense samples with a uniform microstructure. However, the addition of Al to CoSb₃ significantly decreased the HV value of the binary skutterudite CoSb₃, which was reported by Recknagel et al. (2007) to be 608. Furthermore, with the increase in the amount of added Al, the value of HV₀.₁ decreased. This may be attributed to the increase in the area fraction of the grain boundaries with the increase in the added Al.

4.4 Alₓ-added Yb₀.₂₅Co₄Sb₁₂ compositions (x = 0.1, 0.2, 0.3)

From the previous section, the excess amount of Al in the grain boundaries of the CoSb₃ binary skutterudite has shown promise in improving the thermoelectric performance by reducing the thermal conductivity without any major effects on the electrical conductivity or the Seebeck coefficient. Therefore, the doping of CoSb₃ with Al beside heavy atom elements from lanthanide group to improve the transport properties is expected to significantly improve the thermoelectric performance of the skutterudite system. Thus, in this section, Al addition to the Yb₀.₂₅Co₄Sb₁₂ ternary skutterudite matrix will be investigated.

It is interesting to discuss other similar structures for a deep understanding of the crystal formation of this type of composition. However, there are many possibilities of forming secondary phases in the skutterudite samples in relation to either the fabrication process or to the non-stoichiometric ratios of the elements in the composition. For example, Yb₀.₂Co₄Sb₁₂ sintered by SPS and discussed by Li et al. (2009) showed a small amount of CoSb₂ impurity, as a result of the short sintering time (5 min), in which the phase transition was not completely accomplished. The same composition investigated
by Peng et al. (2009) showed a single phase of skutterudite when sintered for 20 min. However, the pre-sintering process plays an important role in the purity of the skutterudite phase; for example, the mechanical alloying process may cause some elements in the composition to form an oxidized secondary phase. Moreover, sublimation of some elements during the melting or sintering processes and the formation of secondary phases in the skutterudite matrix are possible causes of deviations in the nominal and actual stoichiometry; i.e., Yb$_2$O$_3$, YbSb and InSb phases were formed in the skutterudite matrix of Yb$_{0.2}$In$_{0.2}$Co$_4$Sb$_{12}$ in the work of Ballikaya et al. (2012).

4.4.1 Microstructural properties

The XRD of the as-sintered samples shown in Figure 4.20 indicates that the influence of the spark plasma sintering process on the metastable MA powders was very efficient. As a result, the MA powders were highly compacted to a polycrystalline skutterudite phase with a very small amount of an AlSb secondary phase. The presence of AlSb was found to vary according to the amount of Al added to the Yb$_{0.25}$Co$_4$Sb$_{12}$ ternary skutterudite system. The AlSb peak that appeared in the Al$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample increased in the Al$_{0.2}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample to record a higher AlSb content among all samples. However, increasing the amount of Al added in the Al$_{0.3}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample caused the peak of the AlSb secondary phase to almost disappear. This result might be attributed to the microstructure of the samples that formed during the SPS process, which can be further elucidated by the SEM and EDX characterizations. However, the small diffraction peak of AlSb indicates that a solid solution of Al in the lattice could be present. Therefore, the lattice parameters were changed accordingly with the change in the amount of the AlSb phase in the structure of Al$_x$Y$_{0.25}$Co$_4$Sb$_{12}$ ($x = 0.1, 0.2$ and $0.3$), which was 9.0471 Å, 9.0506 Å and 9.0475 Å, respectively. The volume fractions of AlSb in the lattice were estimated using HighScore Plus software. The software indicated that less than 0.1 wt. % of AlSb formed in all samples and the major phase was skutterudite.
Figure 4.20: XRD patterns of the as-sintered sample of $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ ($x = 0.1, 0.2, 0.3$).

The SEM micrographs of the as-sintered samples of $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ ($x = 0.1, 0.2$ and 0.3) shown in Figure 4.21(a), Figure 4.22(a) and Figure 4.23(a), respectively, indicate two types of surface topographies. The first topography involves an aggregation of grains in the form of solid islands with very narrow grain boundaries. The second topography involves the formation of individual grains surrounded by relatively wide grain boundaries. These grain islands varied in terms of quantity and size according to the amount of Al added. The number of grain islands decreased with the increase in the amount of Al added associated with a shrinkage in size. Therefore, the presence of more individual grains was realized. Moreover, the average size of the individual grains decreased linearly with the evolution of new individual grains caused by the addition of Al. Thus, small grains with a large area fraction of grain boundaries might lead to a
scattering of the Al atoms among the grain boundaries and hence reduce the possibility of the formation an AlSb phase. This phenomenon could be the reason behind the reduction of the AlSb peak observed in the XRD analysis of Al0.3Yb0.25Co4Sb12.

The presence of an AlSb phase was verified in the grain boundaries of all samples using SEM/EDS. Moreover, elemental mapping was utilized to further investigate the microstructure and actual composition of the samples. The elemental mapping of the as-sintered samples of AlxYb0.25Co4Sb12 (x = 0.1, 0.2 and 0.3) shown in Figures 4.21(c, d, e, f), Figures 4.22(c, d, e, f) and Figures 4.23(c, d, e, f), respectively, clearly illustrates the distribution of the quaternary system elements. Yb, Co and Sb were distributed in a systematic order in the surface of the grains of the as-sintered samples, whereas Al was less present inside the grains but had a strong presence in the grain boundaries beside Sb. This result may confirm that the skutterudite phase indicated by XRD belongs to the formation of a filled-skutterudite phase in the grains partially filled by Yb atoms. Moreover, the presence of Al beside Sb in the grain boundaries agrees with the AlSb peak indicated in the XRD graph. The Al atoms that appeared as rich spots in the grain boundaries of Al0.1Yb0.25Co4Sb12 in Figure 4.21(c) tend to scatter among the wide grain boundaries of Al0.2Yb0.25Co4Sb12 in Figure 4.22(c). The scattering of Al atoms reached their maximum mode in Al0.3Yb0.25Co4Sb12 in Figure 4.23(a), when the area fraction of the grain boundaries increased as a result of the production of new grains associated with the shrinkage of the average grain size. Thus, a very tiny amount of Al-rich aggregates in the grain boundaries of Al0.3Yb0.25Co4Sb12 in Figure 4.23(c) were detected. However, in recent studies, InSb clusters have appeared as a secondary phase in In-doped CoSb3, rather than entering the Sb-icosahedral voids, with demonstrated improvements in electrical performance and consequently TE efficiencies (Graff et al., 2011; Li et al., 2009; Peng et al., 2009).
Figure 4.21: SEM images of Al$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, (b) an SEM/EDX micrograph, and (c) integrated elemental mapping; the elemental mapping of (d), (e), (f) and (g) show Al, Yb, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.22: SEM images of Al$_{0.2}$Yb$_{0.25}$Co$_4$Sb$_{12}$: (a) a micrograph of an SPS-compacted sample, (b) an SEM/EDX micrograph, and (c) integrated elemental mapping; the elemental mapping of (d), (e), (f) and (g) show Al, Yb, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.23: SEM images of Al$_{0.3}$Yb$_{0.25}$Co$_{4}$Sb$_{12}$; (a) a micrograph of an SPS-compact sample, (b) an SEM/EDX micrograph, and (c) integrated elemental mapping; the elemental mapping of (d), (e), (f) and (g) show Al, Yb, Co, and Sb, respectively, extracted from (b) using EDX.
4.4.2 Thermoelectric properties

The temperature dependence of electrical resistivity for the Al$_x$Yb$_{0.25}$Co$_4$Sb$_{12}$ ($x=0.1,$ 0.2 and 0.3) samples shown in Figure 4.24(a) demonstrate a very low electrical resistivity for all compositions compared with single-phase Yb$_{0.2}$Co$_4$Sb$_{12}$ (11.4 $\mu$Ωm) (Li et al., 2009) at room temperature. The electrical resistivity of the compositions increased with increasing temperature, indicating a metal-like behavior over the entire temperature range for all samples. This behavior is typically similar to the In$_x$Yb$_{0.2}$Co$_4$Sb$_{12}$ compositions discussed in the work of Peng et al. (2009). The electrical resistivity range was very narrow for all samples, i.e., minimum electrical resistivities of 5.5 $\mu$Ωm, 5.3 $\mu$Ωm and 7.6 $\mu$Ωm at room temperature and maximum electrical resistivities of 10.9 $\mu$Ωm, 9.3 $\mu$Ωm and 10.5 $\mu$Ωm at 577 °C were recorded for Al$_x$Yb$_{0.25}$Co$_4$Sb$_{12}$ ($x=0.1, 0.2$ and 0.3), respectively. The average value of electrical resistivity decreased with an increasing amount of AlSb nano-inclusions in the composition. Referring back to section 4.4.1, the maximum AlSb content was found in the Al$_{0.2}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition, which exhibited the minimum electrical resistivity among all compositions. This correlation disagrees with the result for Yb$_x$Co$_4$Sb$_{12}$/yGaSb in the work of Xiong et al. (2010) and Yb$_{0.2}$Co$_4$Sb$_{12}$/xPbTe in the work of Liu et al. (2011), in which the nano-inclusions increased the electrical resistivity. However, the high impurities and defects of the Al and AlSb nano-inclusions present in the crystal lattice of Al$_{0.3}$Yb$_{0.25}$Co$_4$Sb$_{12}$ may cause new additional electronic states within the bandgap and trap the charge carriers. Therefore, a suitable and controlled amount of AlSb nano-inclusions in the lattice of filled CoSb$_3$ skutterudite may significantly enhance the electrical conductivity.

Figure 4.24(b) shows the temperature dependence of the Seebeck coefficient for Al$_x$Yb$_{0.25}$Co$_4$Sb$_{12}$ ($x=0.1,$ 0.2 and 0.3). A high Seebeck coefficient of -217 $\mu$V/K for the Al$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample was recorded at 577 °C. This value was reduced at the same temperature to -207 $\mu$V/K for the Al$_{0.2}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample. A small increase in the
Seebeck coefficient value of -212 $\mu$V/K was realized with the increase in the addition of Al in the $\text{Al}_{0.3}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ sample. The negative sign of the Seebeck coefficient values for all samples indicates n-type behavior. The Seebeck coefficient is strongly associated with the mean carrier energy near the Fermi level (Liu et al., 2011). Therefore, although the electrical resistivity is low, a high Seebeck coefficient is speculated for all compositions, attributed to the scattering of low-energy electrons by the grain-boundary potential barrier, which appears to be the dominant scattering mechanism. Martin et al. (2009) proposed that the carrier trapping in the grain boundaries forms energy barriers that impede the conduction of carriers between grains, essentially filtering charge carriers with energy less than the barrier height.

A very high and stable operating range of power factors was obtained for $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ ($x = 0.1, 0.2$ and 0.3), as shown in Figure 4.24(c). The highest power factor of $4.9 \times 10^{-3}$ W/m.K$^2$ belonged to the $\text{Al}_{0.1}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ sample at 377 °C. A small reduction of this value was realized at a lower temperature of 327 °C to be $4.7 \times 10^{-3}$ W/m.K$^2$ for the $\text{Al}_{0.2}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ sample. With the increase in the Al added to the $\text{Al}_{0.3}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ sample, the maximum power factor value decreased to $4.3 \times 10^{-3}$ W/m.K$^2$ at an elevated temperature of 577 °C.
Figure 4.24: Temperature dependence of the (a) electrical resistivity, (b) Seebeck coefficient, and (c) power factor ($PF$) for Al$_x$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ ($x = 0.1, 0.2, 0.3$) compositions.
In Figure 4.25(a) the temperature dependence of the thermal conductivity \((K)\) is shown for \(\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) \((x = 0.1, 0.2\) and 0.3). The minimum thermal conductivity \((K_{\text{min}})\) for all samples was recorded at the room temperature. The \(K_{\text{min}}\) for the \(\text{Al}_{0.1}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) sample was found to be 3.3 W/m.K, and this value decreased to 3.0 W/m.K for the \(\text{Al}_{0.2}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) sample. A significant reduction in \(K\) of 1.9 W/m.K was obtained for \(\text{Al}_{0.3}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\), the high Al content sample. The gradual increase in the thermal conductivities as a function of temperature for the \(\text{Al}_{0.1}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) and \(\text{Al}_{0.3}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) samples revealed a maximum \(K\) of 4.1 W/m.K and 2.7 W/m.K at 850 K, respectively. The increase in the thermal conductivity of the \(\text{Al}_{0.2}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) sample at low temperatures was gradual up to 500 K and became rapid after 500 K, resulting in a relatively high thermal conductivity at elevated temperatures \((K_{\text{max}} = 4.5\) W/m.K at 850 K). The rapid increase in the \(K\) value after 500 K can be attributed to the effect of bipolar diffusion. The bipolar diffusion effect of electron thermal conductivity is mainly caused by the difference in the energy range of the electrons determining the electron thermal conductivity from that of electrical conductivity. Conversely, the bipolar diffusion effect may be caused by the diffusion of electron-hole pairs moving toward the same direction due to the temperature gradient of the sample. In this state, the charge of electrons and holes compensate each other, and the heat current occurs without causing an electrical current, which makes the Wiedemann-Franz law invalid.

The lattice thermal conductivity, \(K_L\), can be estimated by subtracting the electronic contribution of the Wiedemann-Franz law, \(K_e = LT/\rho\), from the total thermal conductivity, where \(L = 2.45 \times 10^{-8} \text{ V}^2\text{K}^2\) is the Lorenz number (Park & Kim, 2010). As shown in Figure 4.25(b), \(K_L\) was significantly suppressed for all samples compared with the \(K_L\) of the binary skutterudite \(\text{CoSb}_3\). Therefore, the minimum \(K_L\) values were found to be 1.9 W/m.K, 1.3 W/m.K and 0.6 W/m.K at 400 K, 500 K, and 500 K for \(\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}\) \((x = 0.1, 0.2\) and 0.3), respectively. The electronic contribution \(K_e\) is more than 60% of the
total thermal conductivity in this system. It is speculated that the low $K_L$ of the $\text{Al}_{0.3}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ sample might be due to the filling of voids in the skutterudite matrix by some Al atoms in a reciprocal manner as the Yb filler in the skutterudite matrix. The interaction between the localized modes of the two different fillers, which have sufficiently different frequencies, and the heat-carrying acoustic phonon modes might strongly scatter a broader spectrum of heat-carrying phonons.

The composites of $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}/\text{AlSb}$ demonstrated a low electrical resistivity, a high Seebeck coefficient and a low lattice thermal conductivity, and this can be attributed to the phenomenological properties of the nanometer length scales of AlSb, including enhanced interfacial phonon scattering and charge carrier filtering. Therefore, high figures of merit $ZT$s of 0.93, 0.87 and 1.36 at different operating temperatures of 800 K, 850 K and 850 K were obtained (see Figure 4.25(c)) for $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ ($x = 0.1, 0.2$ and 0.3), respectively. Remarkably, the composites of $\text{Al}_x\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ with AlSb nano-inclusions yielded excellent results in terms of a fast fabrication process compared with the composition of $\text{Yb}_{0.2}\text{Co}_4\text{Sb}_{12}$ with PbTe inclusions, which showed a lower ZT value of 0.78 at 700 K when prepared by the ball-milling and hot-pressing process (Liu et al., 2011).
Figure 4.25: Temperature dependence of the (a) thermal conductivity, (b) lattice thermal conductivity, and (c) Figure of merit $ZT$ for Al$_{x}$-added Yb$_{0.25}$Co$_{4}$Sb$_{12}$ ($x = 0.1, 0.2, 0.3$) compositions.
4.4.3 Thermal behavior

Figures 4.26 and 4.27 give the thermal stability of the Al$_x$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions ($x = 0.1, 0.2, 0.3$). The TGA thermographs in Figures 4.26(a), 4.26(b), and 4.26(c) show great stability of the $x = 0.1, 0.2$, and 0.3 compositions up to 547 °C, 530 °C, and 521 °C, respectively. A small amount of weight loss can be observed from 547 °C to 586 °C, from 530 °C to 554 °C, and from 530 °C to 554 °C for the $x = 0.1, 0.2$, and 0.3 compositions, respectively, attributed to the sublimation of impurities in the starting materials and/or the evaporation of the moisture gained during sample preparation for STA. Gradual weight loss above 644 °C for all compositions was realized as a result of the sublimation of Sb. Decomposition of the skutterudite phase was observed at 872 °C, 858 °C, and 852 °C for the $x = 0.1, 0.2$, and 0.3 compositions, respectively.

The DSC thermographs shown in Figures 4.27(a), 4.27(b) and 4.27(c) indicate two endothermic peaks for all compositions corresponding to the skutterudite phase and AlSb phase. The onset melting point was observed to be over 800 °C for all samples, which can be attributed to the skutterudite phase. A clear onset melting point of the AlSb phase was realized at 893 °C, 875 °C, and 867 °C for the $x = 0.1, 0.2$ and 0.3 compositions, respectively.
Figure 4.26: TGA thermographs upon heating of Al$_x$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions: (a) $x = 0.1$, (b) $x = 0.2$, and (c) $x = 0.3$. 
Figure 4.27: DSC thermographs upon heating (red line) and cooling (blue line) of the Al\textsubscript{x}-added Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} compositions: (a and b) x = 0.1, (c and d) x = 0.2, and (e and f) x = 0.3.
4.4.4 Mechanical properties

To assess the homogeneity of the Al\textsubscript{x}-added Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} samples (x = 0.1, 0.2, and 0.3), micro-hardness was mapped on several cross-sections of the specimens. A homogeneous distribution of HV\textsubscript{0.1} with average values of 475, 456, and 441 were observed for Al\textsubscript{x}-added Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} compositions (x = 0.1, 0.2, and 0.3), respectively. There were no significant differences between the different regions of the samples’ margins and interior areas, thus emphasizing the suitability of the SPS process for producing dense samples with a uniform microstructure. Furthermore, with the increase in the amount of added Al, the value of HV\textsubscript{0.1} decreased. This may be attributed to the increase in the area fraction of the grain boundaries with the increase in the added Al.

4.5 Al\textsubscript{x}Bi\textsubscript{y}-added Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} compositions ((x, y) = (0.1,0), (0, 0.1), (0.1,0.05))

From the previous section, the excess amount of light elements from other metal groups (Al) in the grain boundaries of the Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} ternary skutterudite matrix greatly improved the thermoelectric performance by reducing the thermal conductivity and electrical resistivity, while maintaining a high Seebeck coefficient value. Therefore, doping a larger and heavier atom from other metal groups, such as Bi, into CoSb\textsubscript{3} beside heavy atoms from the lanthanide group is expected to improve the overall thermoelectric parameters. Thus, in this section, the addition of Al to the Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} ternary skutterudite matrix will be compared with the addition of Bi and Al-Bi to the same matrix.

4.5.1 Microstructural properties

Figure 4.28 shows the XRD patterns of the Al\textsubscript{x}Bi\textsubscript{y}-added Yb\textsubscript{0.25}Co\textsubscript{4}Sb\textsubscript{12} compositions of ((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05)). Sharp peaks were observed for all samples, indicating their crystalline nature. For the sample with (x, y) = (0.1, 0), sharp peaks of the skutterudite phase were indicated with a small peak of the secondary AlSb phase. The
same behavior was observed for the sample with \((x, y) = (0, 0.1)\), which had a polycrystalline skutterudite phase with a small amount of Bi as a secondary phase. Conversely, the combination of the two dopants in one sample demonstrated a polycrystalline skutterudite phase with AlSb and Bi as secondary phases when \((x, y) = (0.1, 0.05)\). The lattice parameters were 9.0471 Å, 9.0384 Å and 9.0374 Å for Al\(_x\)Bi\(_y\)-added Yb\(_{0.25}\)Co\(_{4}\)Sb\(_{12}\) compositions of \(((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05))\), respectively. The shrinkage of the lattice parameter can be attributed to the point defects caused by the Al and Bi doping. Obviously, the lattice contraction was proportional to the atomic size of the dopant and the amount of the secondary phases. For example, Bi has a relatively larger radii than Al, and, as a result, the sample that containing Bi has a smaller lattice parameter value than the one containing Al. Therefore, the availability of both dopants in one sample might increase the number of point defects and thus lead to more contraction in the lattice parameter, i.e., the \((x, y) = (0.1, 0.05)\) sample. The fractions of AlSb and Bi in the lattice were estimated using HighScore Plus software. The software indicated that less than 0.1 wt\% of the secondary phase’s composition was formed in all samples, while the major phase was skutterudite. Thus, this may indicate that some free Al and Bi were lost in the ball-milling process and/or were squeezed out during the spark plasma sintering process.
Figure 4.28: XRD patterns of the as-sintered sample of Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions: (a) $x = 0.1$ and $y = 0$, (b) $x = 0$ and $y = 0.1$, and (c) $x = 0.1$ and $y = 0.05$.

Figures 4.21, 4.29 and 4.30 display the microstructures and compositions of the Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions of $((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05))$. Homogenous composites were observed in the backscattered electron image, as shown in Figures 4.21(a), 4.29(a) and 4.30(a). As in Figure 4.21(a) for $(x, y) = (0.1, 0)$, an agglomeration of large grains in the form of islands was distributed over the entire sample region with small individual grains in between. In the $(x, y) = (0, 0.1)$ sample, as shown in Figure 4.29(a), large grains were detected, and some point defects were observed inside the grains. The texture changed significantly, as shown in Figure 4.30(a), when two dopants were used in the $(x, y) = (0.1, 0.05)$ sample. Small grains with several point defects were found to be the main feature of the Al-Bi-doped sample. However, light
atoms such as Al had less of an impact on the surface microstructure than did heavy atom such as Bi.

The elemental mapping of Al, Yb, Co and Sb shown in Figures 4.21(c, d, e, f, g) for the (x, y) = (0.1, 0) sample shows a highly uniform dispersion of Yb, Co and Sb, while an Al-rich spot was detected in the grain boundaries. A highly uniform dispersion of Yb, Co and Sb was also recorded for the (x, y) = (0, 0.1) sample inside the grains, as shown in Figures 4.29(c, d, e, f, g). Conversely, the absence of these ternary system elements was observed at some points in the grain boundaries to be occupied by Bi. In the quintuple system of (x, y) = (0.1, 0.05), the composition of which is shown in Figures 4.30(c, d, e, f, g), the elemental mapping shows a highly uniform dispersion of Yb, Co and Sb inside the grains. Conversely, Bi agglomerated along the grain boundaries and distributed evenly in the form of small spots inside the grains, while less agglomeration was detected for Al, which appeared as small Al-rich spots in the grain boundaries as well as inside the grains. In comparison, the addition of Bi to CoSb₃ in the work of Mallik et al. (2013) demonstrated that the Bi atom was found neither as a filler of the voids in the 2a sites nor as a substitute for Sb sites in the 24g sites of the skutterudite matrix; it was only found as a secondary phase.
Figure 4.29: SEM images of Bi$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$, (a) a micrograph of SPS-compacted sample, (b) an SEM/EDX micrograph, and (c) integrated elemental mapping; the elemental mapping of (d), (e), (f) and (g) show Bi, Yb, Co, and Sb, respectively, extracted from (b) using EDX.
Figure 4.30: SEM images of Al$_{0.1}$Bi$_{0.05}$Yb$_{0.25}$Co$_4$Sb$_{12}$, (a) a micrograph of an SPS-compacted sample, (b) SEM/EDX micrograph; the elemental mapping of (c), (d), (e), (f) and (g) show Al, Bi, Yb, Co, and Sb, respectively, extracted from (b) using EDX.
4.5.2 Thermoelectric properties

The temperature dependence of the electrical resistivity of the $\text{Al}_x\text{Bi}_y$-added $\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ compositions of $((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05))$ are shown in Figure 4.31(a). Generally, the addition of Al resulted in a very low electrical resistivity at room temperature compared with the addition of Bi. Moreover, the electrical resistivity of the composition with Al doping increased with increasing temperature, indicating a metallic behavior over the entire temperature range. The electrical resistivity of the composition with Bi doping decreased with increasing temperature, indicating a semiconductor behavior over the entire temperature range.

In addition, the range of the electrical resistivity was very narrow for the Al-doped sample, i.e., a minimum electrical resistivity of 5.5 $\mu\Omega$m at room temperature and a maximum electrical resistivity of 10.9 $\mu\Omega$m at 577 °C was recorded for $\text{Al}_{0.1}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$. The range of the electrical resistivity was relatively wide for the Bi-doped sample, i.e., a minimum electrical resistivity of 30 $\mu\Omega$m at 427 °C and a maximum electrical resistivity of 122 $\mu\Omega$m at room temperature was recorded for $\text{Bi}_{0.1}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$. However, a narrow range of electrical resistivity for the $\text{Al}_{0.1}\text{Bi}_{0.05}\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ composition was demonstrated, i.e., a minimum electrical resistivity of 22 $\mu\Omega$m at room temperature and a maximum electrical resistivity of 35 $\mu\Omega$m at 377 °C. This sample exhibited semiconductor behavior from room temperature until 377 °C, at which point the behavior changed to a metal-like behavior. The presence of an electrically active impurity such as Bi would offset the carrier balance; thus, the formation of impurity levels might cause the structure to turn into a degenerate semiconductor with a metal-like electrical resistivity with a rise in temperature.

Figure 4.31(b) shows the temperature dependence of the Seebeck coefficient for $\text{Al}_x\text{Bi}_y$-added $\text{Yb}_{0.25}\text{Co}_4\text{Sb}_{12}$ compositions of $((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05))$. A
high Seebeck coefficient of -217 µV/K was demonstrated for the Al$_{0.1}$Y$_{0.25}$Co$_4$Sb$_{12}$ sample at 577 °C. The negative sign that appeared in the Seebeck coefficient values indicates n-type behavior. The Bi-doping in the Bi$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition demonstrated a higher Seebeck coefficient value of 307 µV/K at 77 °C, with a positive sign for all values over the entire temperature range, indicating p-type behavior. Thus, addition of Al increased the electron concentration, while the addition of Bi increased the concentration of holes. The Seebeck coefficient value was boosted to 409 µV/K at 277 °C for the Al$_{0.1}$Bi$_{0.05}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition. A negative sign accompanied all values over the entire temperature range, reflecting n-type behavior. A Seebeck coefficient value of -248 µV/K at 127 °C was demonstrated for Bi$_{0.05}$Co$_4$Sb$_{12}$ in Mallik et al. (2013). Therefore, the addition of Al and Bi together in the ternary skutterudite system would significantly boost the Seebeck value rather compared to using only one of these elements. Martin et al. (2009) suggested that the availability of the secondary phases may result in an increased trapping of carriers at grain boundaries, which would form energy barriers that shackle the conduction of carriers between grains. A potential barrier in the grain boundary might lead to a high Seebeck coefficient.

In Figure 4.31(c), the power factors for Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions of ((x, y) = (0.1,0), (0, 0.1), (0.1,0.05)) are highlighted. A stable power factor operating range was obtained for Al$_{0.1}$Y$_{0.25}$Co$_4$Sb$_{12}$, with a maximum PF of 4.9×10$^{-3}$ W/m.K$^2$ at 377 °C. A relatively low power factor of 1.3×10$^{-3}$ W/m.K$^2$ at a lower temperature of 277 °C was obtained for the Bi$_{0.1}$Y$_{0.25}$Co$_4$Sb$_{12}$ sample. A very high power factor of 5×10$^{-3}$ W/m.K$^2$ was obtained at 227 °C for Al$_{0.1}$Bi$_{0.05}$Y$_{0.25}$Co$_4$Sb$_{12}$. 

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Figure 4.31: Temperature dependence of the (a) electrical resistivity, (b) Seebeck coefficient, and (c) power factor (PF) for \( \text{Al}_x\text{Bi}_y \)-added \( \text{Yb}_{0.25}\text{Co}_{4}\text{Sb}_{12} \) compositions: (a) \( x = 0.1 \) and \( y = 0 \), (b) \( x = 0 \) and \( y = 0.1 \), and (c) \( x = 0.1 \) and \( y = 0.05 \).
In Figure 4.32(a), the temperature dependence of the thermal conductivity ($K$) is demonstrated for $Al_xBi_y$-added $Yb_{0.25}Co_4Sb_{12}$ compositions of $((x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05))$. The minimum thermal conductivity ($K_{min}$) for the compositions was recorded at different temperatures. The $K_{min}$ for the $Al_{0.1}Yb_{0.25}Co_4Sb_{12}$ sample was found to be 3.3 W/m.K at room temperature, while this value significantly decreased for the $Bi_{0.1}Yb_{0.25}Co_4Sb_{12}$ sample to 2.4 W/m.K at an elevated temperature of 850 K. The minimum $K$ value of 2.8 W/m.K at 500 K was obtained for $Al_{0.1}Bi_{0.05}Yb_{0.25}Co_4Sb_{12}$. Over the entire temperature range, the sample with Al and Bi together had a $K$ value that was almost average among the samples with a single dopant of either Al or Bi.

Starting from room temperature, the gradual increase in the thermal conductivity as a function of temperature was indicated for the $Al_{0.1}Yb_{0.25}Co_4Sb_{12}$ composition to a $K_{max}$ of 4.1 W/m.K at 850 K. The opposite behavior of temperature-dependent thermal conductivity was detected for $Bi_{0.1}Yb_{0.25}Co_4Sb_{12}$. A $K_{max}$ of 4.9 W/m.K was recorded at room temperature, and a linear drop in the $K$ value with the increase in temperature was then demonstrated until an elevated temperature of 850 K. A combination of the two different behaviors was observed for the $Al_{0.1}Bi_{0.05}Y_{0.25}Co_4Sb_{12}$ composition. The sample exhibited a decrease in thermal conductivity until 500 K, at which point the reverse behavior occurred; a gradual increase in the $K$ value was observed to a $K_{max}$ of 3.7 W/m.K at 850 K. The same behavior of increasing thermal conductivity was observed above 650 K in the triple-filled skutterudites ($Ba_xYb_yIn_zCo_4Sb_{12}$) studied by Ballikaya et al. (2010) and was attributed to the electronic term.

The lattice thermal conductivity, $K_L$, can be estimated by subtracting the electronic contribution of the Wiedemann-Franz law, $K_e = LT/\rho$, from the total thermal conductivity, where $L = 2.45 \times 10^{-8} \text{ V}^2\text{K}^2$ is the Lorenz number (Park & Kim, 2010). As shown in Figure 4.32(b), $K_L$ was significantly suppressed for all samples compared with the $K_L$ of
the binary skutterudite CoSb$_3$. The effect of $K_e$ was significant in the Al$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ sample, where a minimum $K_L$ value of 1.9 W/m.K was observed at 400 K. However, a significant effect of $K_L$ was observed for the Bi$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition, with a minimum $K_L$ value of 1.7 W/m.K at an elevated temperature of 850 K. In the Al$_{0.1}$Bi$_{0.05}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition, the $K_L$ was relatively high at 2.4 W/m.K at 600 K as a minimum lattice thermal conductivity.

As observed in Figure 4.32(c), the Al$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ composition demonstrated a low electrical resistivity, high Seebeck coefficient and low lattice thermal conductivity. Therefore, a high figure of merit $ZT$ of 0.93 at 800 K was obtained. Bi$_{0.1}$Yb$_{0.25}$Co$_4$Sb$_{12}$ demonstrated a relatively high electrical resistivity, high Seebeck coefficient and moderated lattice thermal conductivity. Therefore, a relatively low Figure of merit $ZTs$ of 0.4 at 850 K was obtained. Al$_{0.1}$Bi$_{0.05}$Yb$_{0.25}$Co$_4$Sb$_{12}$ demonstrated a moderate electrical resistivity, very high Seebeck coefficient and relatively high lattice thermal conductivity. Therefore, a Figure of merit $ZT$ of 0.9 at 600 K was obtained.
Figure 4.32: Temperature dependence of the (a) thermal conductivity, (b) lattice thermal conductivity, and (c) Figure of merit $ZT$ for $Al_xBi_y$-added $Yb_{0.25}Co_{4}Sb_{12}$ compositions: (a) $x = 0.1$ and $y = 0$, (b) $x = 0$ and $y = 0.1$, and (c) $x = 0.1$ and $y = 0.05$. 
4.5.3 Thermal behavior

Figures 4.33 and 4.34 indicate the thermal stability of Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions of (x, y) = (0.1, 0), (0, 0.1), and (0.1, 0.05). The TGA thermograph in Figures 4.33(a), 4.33(b), and 4.33(c) shows great stability of the (x, y) = (0.1, 0), (0, 0.1), and (0.1, 0.05) compositions up to 547 °C, 533 °C, and 533 °C, respectively. A small amount of weight loss can be observed from 547 °C to 586 °C, from 533 °C to 561 °C, and from 533 °C to 553 °C for the (x, y) = (0.1, 0), (0, 0.1), and (0.1, 0.05) compositions, respectively, attributed to the sublimation of impurities in the starting materials and/or the evaporation of the moisture gained during sample preparation for STA. Gradual weight loss above 644 °C was realized for all compositions as a result of the sublimation of Sb. Decomposition of the skutterudite phase was observed at 872 °C, 865 °C, and 872 °C for the (x, y) = (0.1, 0), (0, 0.1), and (0.1, 0.05) compositions, respectively.

The DSC thermographs of Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions of (x, y) = (0.1, 0), (0, 0.1), and (0.1, 0.05) are shown in Figure 4.34. Figure 4.34(a) indicates two endothermic peaks for the (x, y) = (0.1, 0) composition, corresponding to onset melting points of the skutterudite phase and AlSb phase at over 800 °C and 890 °C, respectively. From Figure 4.34(b), an onset melting point of over 800 °C was obtained for (x, y) = (0, 0.1), which can be attributed to the skutterudite phase. In addition, there were other sub-endothermic peaks for the melting of the residual phases after decomposition. From Figure 4.34(c), an onset melting point at over 800 °C was obtained for (x, y) = (0.1, 0.05), which can be attributed to the skutterudite phase. In addition, there were other sub-endothermic peaks for the melting of the residual phases after decomposition.
Figure 4.33: TGA thermographs upon heating (red line) and cooling (blue line) of the Al₆Bi₆-added Yb₀.₂₅Co₄Sb₁₂ compositions: (a) x = 0.1 and y = 0, (b) x = 0 and y = 0.1, and (c) x = 0.1 and y = 0.05.
Figure 4.34: DSC thermographs upon heating (red line) and cooling (blue line) of the Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions: (a and b) $x = 0.1$ and $y = 0$, (c and d) $x = 0$ and $y = 0.1$, and (e and f) $x = 0.1$
4.5.4 Mechanical properties

To assess the homogeneity of the Al_{x}Bi_{y}-added Yb_{0.25}Co_{4}Sb_{12} samples (x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05), micro-hardness was mapped on several cross-sections of the specimens. A homogeneous distribution of HV_{0.1} with average values of 475, 430, and 442 was observed for the Al_{x}Bi_{y}-added Yb_{0.25}Co_{4}Sb_{12} compositions of (x, y) = (0.1, 0), (0, 0.1), (0.1, 0.05), respectively. There were no significant differences between the different regions of the samples’ margins and interior areas, thus emphasizing the suitability of the SPS process for producing dense samples with a uniform microstructure. Furthermore, the addition of Bi had a greater impact on the microstructure of the ternary skutterudite system than did the addition of Al. The sample with added Bi had a lower HV_{0.1} value than the sample with added Al. This may be attributed to the higher number of point defects in the Bi-added sample than in the Al-added sample.
CHAPTER 5: CONCLUSIONS AND RECOMMENDATIONS

5.1 Conclusions

Thermoelectric materials for waste-heat recovery, refrigeration and other applications are of great interest because they can serve as a secondary heat generation technology, which leads to a reduction in the global dependency on fossil fuels. Therefore, in this work, novel skutterudite thermoelectric materials which can be used for waste-heat recovery in the aerospace and automobile applications were synthesized and examined in terms of their microstructural, thermoelectric, charge transport, and mechanical properties, as well as the thermal stability of the final products. The following formulations were explored with conclusions that indicate a strategy to increase the thermoelectric figure of merit:

1. A formulation of Mn-added CoSb$_3$ was studied. The fabrication process involved mechanical alloying followed by spark plasma sintering to produce a fully dense sample. Polycrystalline phases of skutterudite with Mn-rich spots in the grain boundaries were obtained. By using small transition metal atoms such as Mn, we were optimistic in significantly decreasing the electrical resistivity as well as the thermal conductivity. However, a tiny reduction in the electrical resistivity from the binary skutterudite CoSb$_3$ was obtained. However, a moderate decrease in the lattice thermal conductivity was observed. Through this work, useful strategies in the modification of binary skutterudites using light elements were initiated.

2. A fully dense sample of Hf-added CoSb$_3$ was synthesized using the mechanical alloying technique followed by spark plasma sintering. Polycrystalline phases of skutterudite were obtained in addition to Hf-rich regions in the grain boundaries. By using relatively small and heavy transition metal cations such as Hf, a similar effect to that of the lanthanide elements was expected. However, a tiny reduction in the electrical resistivity, from the binary skutterudite CoSb$_3$ was obtained.
However, a significant decrease (up to 60%) in the lattice thermal conductivity was observed.

3. Excess doping of Al into CoSb$_3$ was investigated to examine the effect of excess doping on the skutterudite morphology and ultimately the thermoelectric performance. Fully dense samples of a modified skutterudite compound, by addition of Alx (0.3, 0.6, 2), were obtained using mechanical alloying followed by spark plasma sintering. The XRD result showed that the addition of Alx (0.3, 0.6, 2) resulted in the formation of a skutterudite phase with AlSb as a secondary phase. However, EDX indicated islands of a skutterudite phase surrounded by Al-rich spots located in the grain boundaries. Moreover, the addition of Al had a significant effect on the lattice thermal conductivity of CoSb$_3$, which was reduced by ~45% in the case of x = 2. It is believed that grain boundary phonon scattering plays a key role in reducing the thermal conductivity. However, a low figure of merit $ZT$ was obtained as a consequence of a high electrical resistivity. Thus, this work is useful in deriving a pathway for improvement in thermoelectrics through microstructural modification.

More interestingly, for the formulation of Al$_{0.3}$Co$_4$Sb$_{12}$, a spin crossover behavior was observed; this is suggested to occur through the transition from low-spin Co(III) to high-spin Co (III), which results in a reversible conversion from n-type to p-type at temperature of 200 °C. Although the current $ZT$ (= 0.06) is low for this formulation, it might be an interesting pathway to manipulate the p- and n-type properties of a particular skutterudite formulation.

4. Al was doped into the Yb$_{0.25}$Co$_4$Sb$_{12}$ skutterudite system. This formulation was the most successful in achieving the highest $ZT$ (= 1.36) in this work for Al$_x$Yb$_{0.25}$Co$_4$Sb$_{12}$ (x = 0.1, 0.2 and 0.3)
were obtained using the mechanical alloying technique followed by spark plasma sintering. A polycrystalline skutterudite phase was obtained in addition to a small amount of an AlSb secondary phase located in the grain boundaries. The increase in Al doping was correlated to a reduction in thermal conductivity, reaching a maximum reduction of 58% from pure CoSb$_3$ with Al$_{0.3}$ addition. Furthermore, the electrical conductivity was maximal with the Al$_{0.2}$Yb$_{0.25}$Co$_4$Sb$_{12}$ formulation due to the presence of AlSb nano-inclusions. Overall, the key driver of the performance in achieving the maximum ZT for Al$_{0.3}$Yb$_{0.25}$Co$_4$Sb$_{12}$ was through the significant reduction in thermal conductivity and a relatively high magnitude of electrical conductivity.

5. Al and Bi were added to the Yb$_{0.25}$Co$_4$Sb$_{12}$ skutterudite system. Fully dense samples of Al$_x$Bi$_y$-added Yb$_{0.25}$Co$_4$Sb$_{12}$ compositions ((x, y) = (0.1,0), (0, 0.1), (0.1,0.05)) were obtained by mechanical alloying followed by spark plasma sintering. A polycrystalline skutterudite phase was obtained in addition to a small amount of AlSb and Bi as secondary phases located in the grain boundaries. The effect of Bi addition on the lattice thermal conductivity was much more significant that the effect Al addition. This significant effect was reflected negatively in the power factor, as the sample with added Bi demonstrated a relatively low PF, whereas a significant PF was realized for the Al-added sample. Therefore, the combination of free Bi atoms to serve as phonon scatterers with AlSb to serve as carrier traps in the grain boundaries resulted in a very high power factor (5 $\mu$V/K) and a relatively low lattice thermal conductivity (3.2) for the composition of Al$_{0.1}$Bi$_{0.05}$-added Yb$_{0.25}$Co$_4$Sb$_{12}$, yielding a ZT of 0.9.
The overall thermoelectric performance of the individual formulations is presented in table 5.1. We hope that with the different strategies of doping, either through substitution or filling, and grain boundary modification, a way forward in optimizing the figures of merit for CoSb$_3$ skutterudite systems can be realized based on this work.
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<th>No.</th>
<th>Composition</th>
<th>$\rho_{\text{min}}$ (µΩ.m) @ °C</th>
<th>$\alpha_{\text{max}}$ (µV/K) @ °C</th>
<th>$PF$ ($10^{-3}$ W/m.K²) @ K</th>
<th>$K_{\text{min}}$ (W/m.K) @ K</th>
<th>$K_{L_{\text{min}}}$ (W/m.K) @ K</th>
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<th>HV</th>
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<td>1</td>
<td>Mn-added CoSb₃</td>
<td>33.2 @ 577 °C</td>
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<td>52.1 @ 546 °C</td>
<td>153 @ 153 °C</td>
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Table 5.1: Summary of the results
5.2 Recommendations

Optimization of the conditions of the mechanical alloying technique and spark plasma sintering process could lead to improved figures of merit, the amount of dopants that serve as phonon scatterers or that serve as carrier traps in the grain boundaries could be optimized. Hafnium can be doped into binary skutterudite with other elements that are compatible with the skutterudite matrix to insure improvement of the overall parameters. Aluminum addition can be introduced into other ternary skutterudite systems, elements such as silver, gold and copper can be used as energy barriers to improve the efficiency of skutterudite thermoelectric materials, and the final products of this project can be incorporated and integrated into thermoelectric modules for the realization of thermoelectric devices for waste thermal energy harvesting.
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LIST OF PUBLICATIONS AND PAPERS PRESENTED

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